

# Conversion from Shear Vorticity To Curvature Vorticity, Organization of Convection, and Hurricane Genesis

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# Outline

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- ▣ Introduction: Dynamics Review
- ▣ Methodology
- ▣ Model Overview
- ▣ Results
- ▣ Conclusions

# Introduction

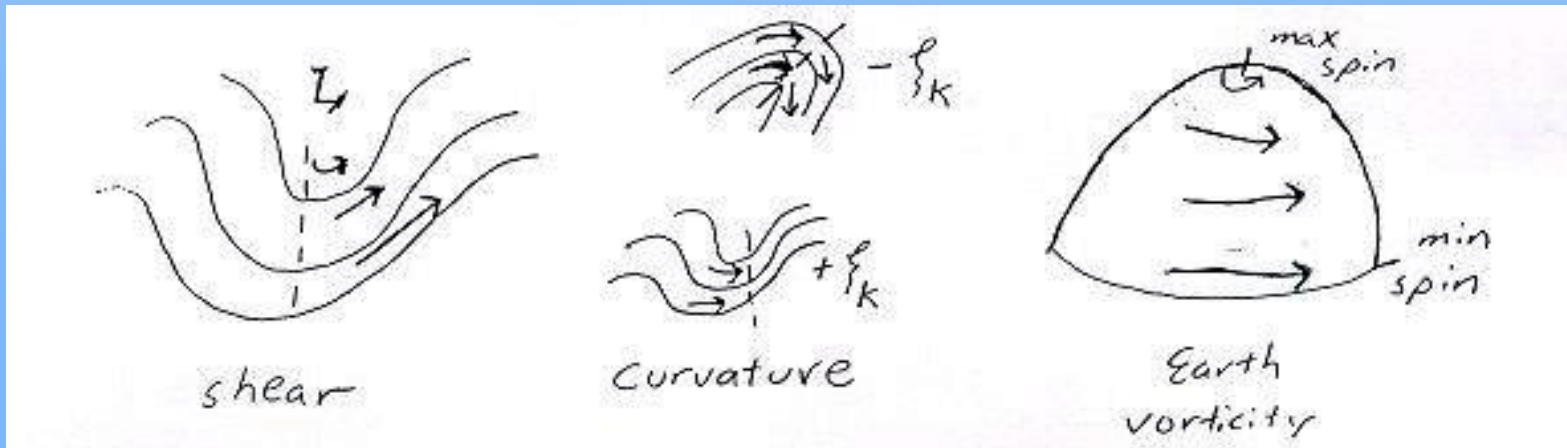
- Krishnamurti et. al. (1986) showed a non-divergent BAROTROPIC model had more skill than persistence for 48 hours over West Africa
- Norquist et. al. (1977) observed that conversion of energy via barotropic processes plays important role in wave maintenance and amplification after wave moves off African continent
- Thorncroft and Hodges (2001) showed correlation between occurrence of 850 mb vorticity centers and frequency of hurricanes in Atlantic
- Ability to predict genesis from AEWs key to improving tropical cyclone forecasts

# Dynamics Review

- Absolute vorticity composed of three components:

1. Shear Vorticity
2. Curvature Vorticity
3. Planetary Vorticity

$$\xi = -\frac{\partial V}{\partial n} + \frac{V}{R} + f$$



Haby, 2007: Example of shear, curvature, and planetary vorticity

# Background Theory

- Study argues importance of barotropic dynamics in the *formation* of a tropical cyclone
- Assuming there are no significant changes in latitude, absolute vorticity is materially conserved:

$$\frac{d\xi}{dt} = 0 = \frac{d\zeta_c}{dt} + \frac{d\zeta_s}{dt}$$

- As shear goes into curvature, parcels will move radially inward towards the center of the disturbance leading to an “organization of convection”
- The concentration of convection will allow for baroclinic based convective processes to further intensify the storm

# Dynamics Review

- Keyser and Bell (1993) derive curvature and shear vorticity tendency equations in natural coordinates:

- Curvature Vorticity Tendency Equation:

$$\frac{d}{dt} \left( f + V \frac{\partial \alpha}{\partial s} \right) = \boxed{\frac{\partial V}{\partial s} \frac{d\alpha}{dt} - \frac{\partial}{\partial n} \left( \frac{\partial \phi}{\partial s} \right)} - \left( f + V \frac{\partial \alpha}{\partial s} \right) \nabla_p \cdot \vec{V} - \vec{V} \frac{\partial \omega}{\partial s} \frac{\partial \alpha}{\partial p}$$

- Shear Vorticity Tendency Equation:

$$\frac{d}{dt} \left( -\frac{\partial V}{\partial n} \right) = \boxed{\frac{\partial V}{\partial s} \frac{d\alpha}{dt} + \frac{\partial}{\partial n} \left( \frac{\partial \phi}{\partial s} \right)} - \left( -\frac{\partial V}{\partial n} \right) \nabla_p \cdot \vec{V} - \vec{V} \frac{\partial \omega}{\partial n} \frac{\partial V}{\partial p}$$

# Methodology

- MM5 used as source for  $u$ ,  $v$ , and  $\varphi$  that are needed for calculating shear vorticity to curvature vorticity conversions for Cartesian coordinates as derived by Bell and Keyser (1993)
- 3 single way nests with resolutions of 27 km, 9 km, and 3 km with 23 unevenly spaced vertical levels
- NCEP  $1^\circ \times 1^\circ$  FNL used for boundary and initial conditions for 27 km domain
- Innermost domain run for 48 hours
- MM5 Model Configuration:
  - Blackadar planetary boundary layer
  - Explicit convection
  - Goddard cloud microphysics
  - Cloud radiation scheme

# Methodology

- Used FSU Barotropic Model initialized with 3 km MM5 data 6 hours into forecast
  - u and v from this time were used to calculate streamfunction
- Model run for total of 42 hours with time step of 1 second
- Study involves developing and non-developing case:
  1. Hurricane Helene (2006): 09/13/06 18Z – 09/15/06 18Z
  2. NAMMA Wave #3 (2006): 08/26/06 12Z – 08/28/06 12Z



# Barotropic Model Review

- Nondivergent barotropic model used:

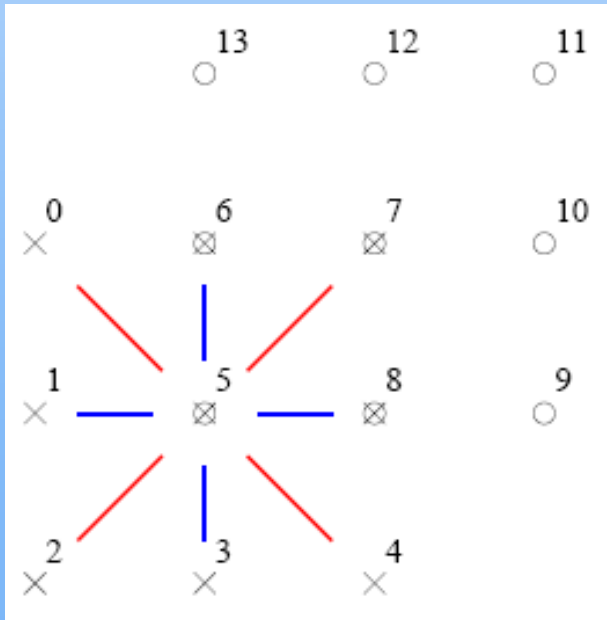
$$\frac{d\xi}{dt} = \frac{\partial \zeta}{\partial t} + J(\psi, \zeta + f) = 0$$

$$J(\psi, \zeta + f) = u \frac{\partial \zeta}{\partial x} + v \frac{\partial \zeta}{\partial y} + \beta v$$

- Relative vorticity generated through movement of parcels to different latitudes

# Barotropic Model Review

- ▣ Advective term calculated using 9-point Arakawa Jacobian



$$J^n = \frac{1}{3} (J_{++} + J_{\times+} + J_{+\times})$$

- ▣ Conserves energy and enstrophy preventing nonlinear instability!

# Matsuno Time Scheme

- Multistep scheme involving “predictor” step and “corrector” step
- Predictor Step: Use forward explicit difference scheme to obtain  $u^{n+1*}$  :

$$u^{n+1*} - u^n = \Delta t g(u^n)$$

- Solve for  $g(u^{n+1*})$  using  $u^{n+1*}$
- Predictor Step: Use  $g(u^{n+1*})$  to solve for  $u^{n+1}$  using backward implicit difference scheme:

$$u^{n+1} - u^n = \Delta t g(u^{n+1*})$$

# Matsuno Time Scheme

## ▣ Advantages:

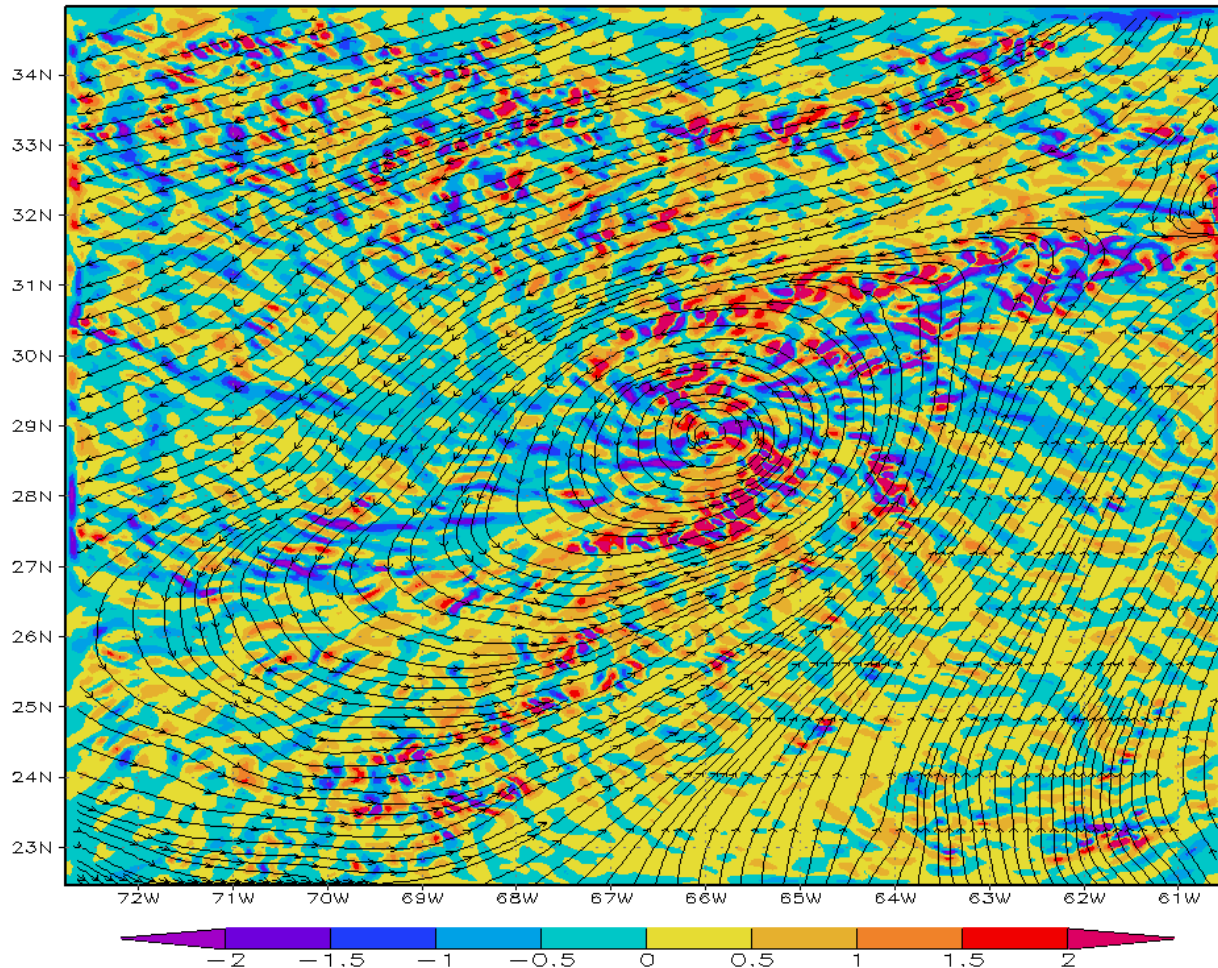
- ▣ higher accuracy: second order accuracy
- ▣ Forward explicit and backward implicit are only first order accurate
- ▣ can use larger time step

## ▣ Disadvantage:

- ▣ computationally expensive because evaluating  $g(u^n)$  several times

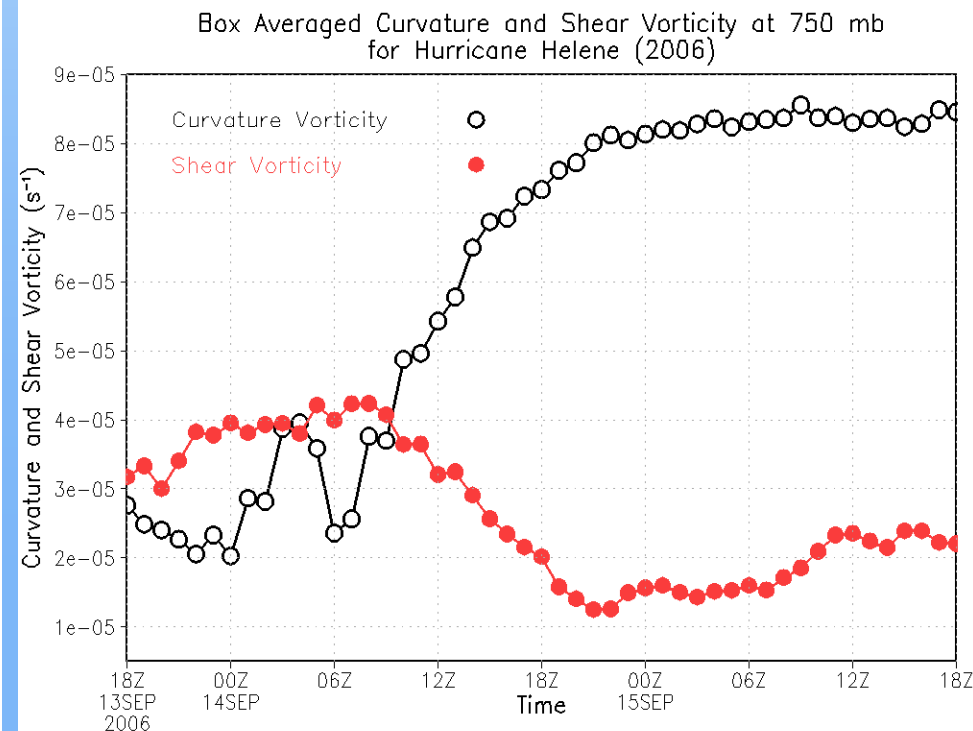
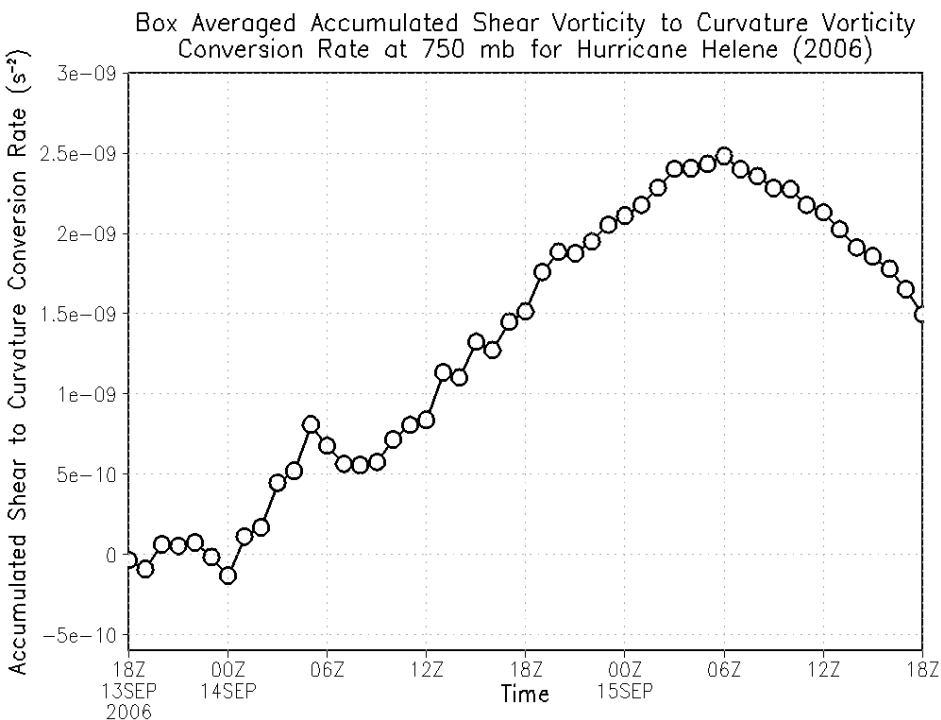
# Shear Vorticity Conversions To Curvature Vorticity Conversions

850 mb S2C Conversion 09/07 03Z ( $10^{-10} \text{ s}^{-2}$ )



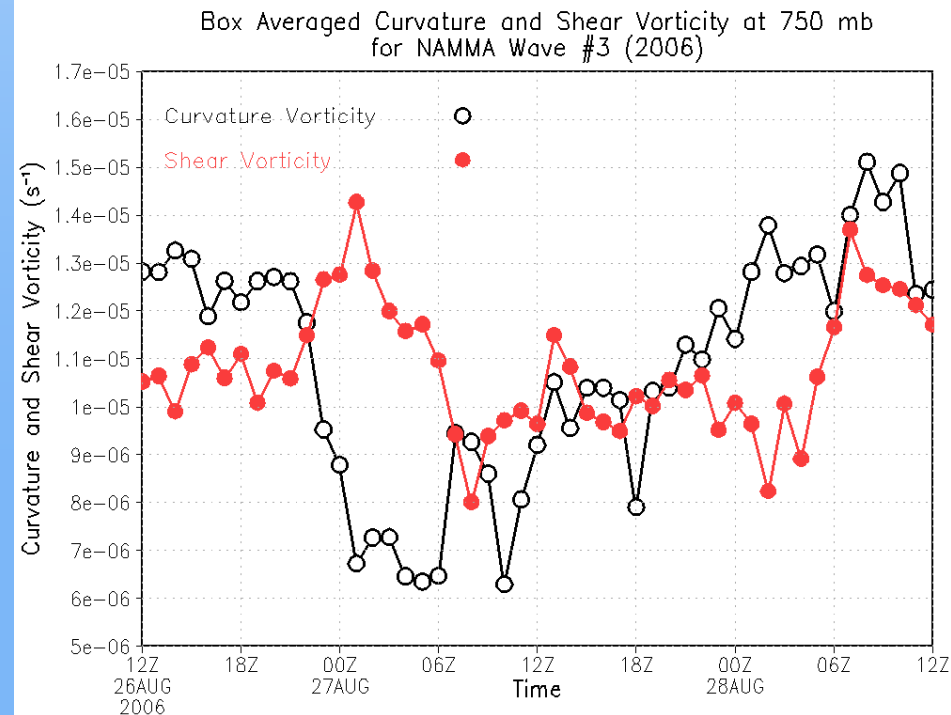
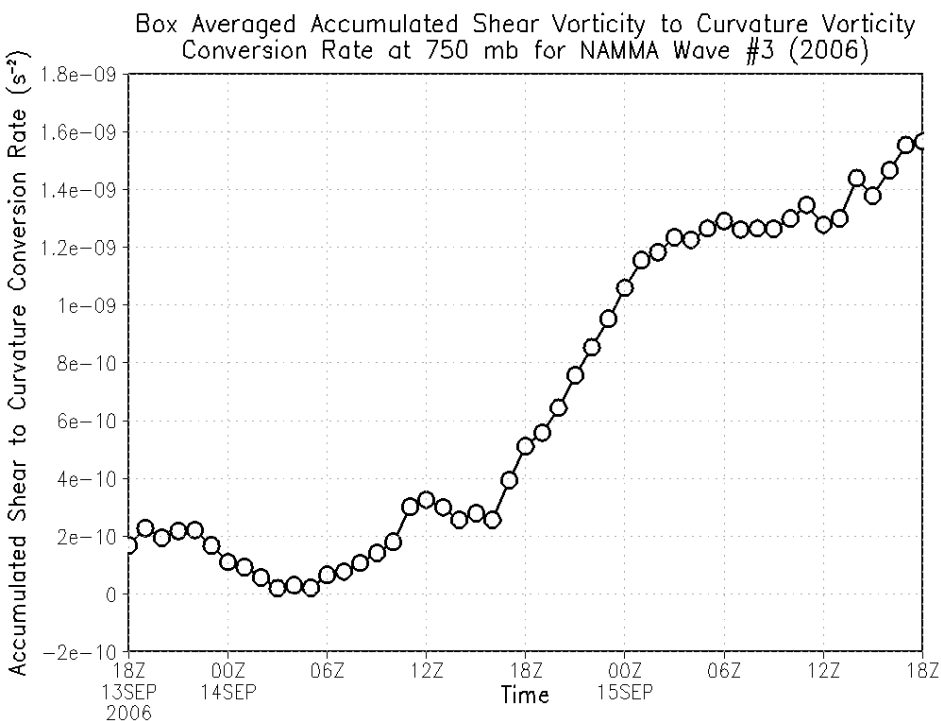
# Accumulated Shear to Curvature for MM5 Run for Hurricane Helene

- Notice consistent conversion of shear vorticity to curvature vorticity in developing case
- Mutual exchange of shear vorticity and curvature vorticity



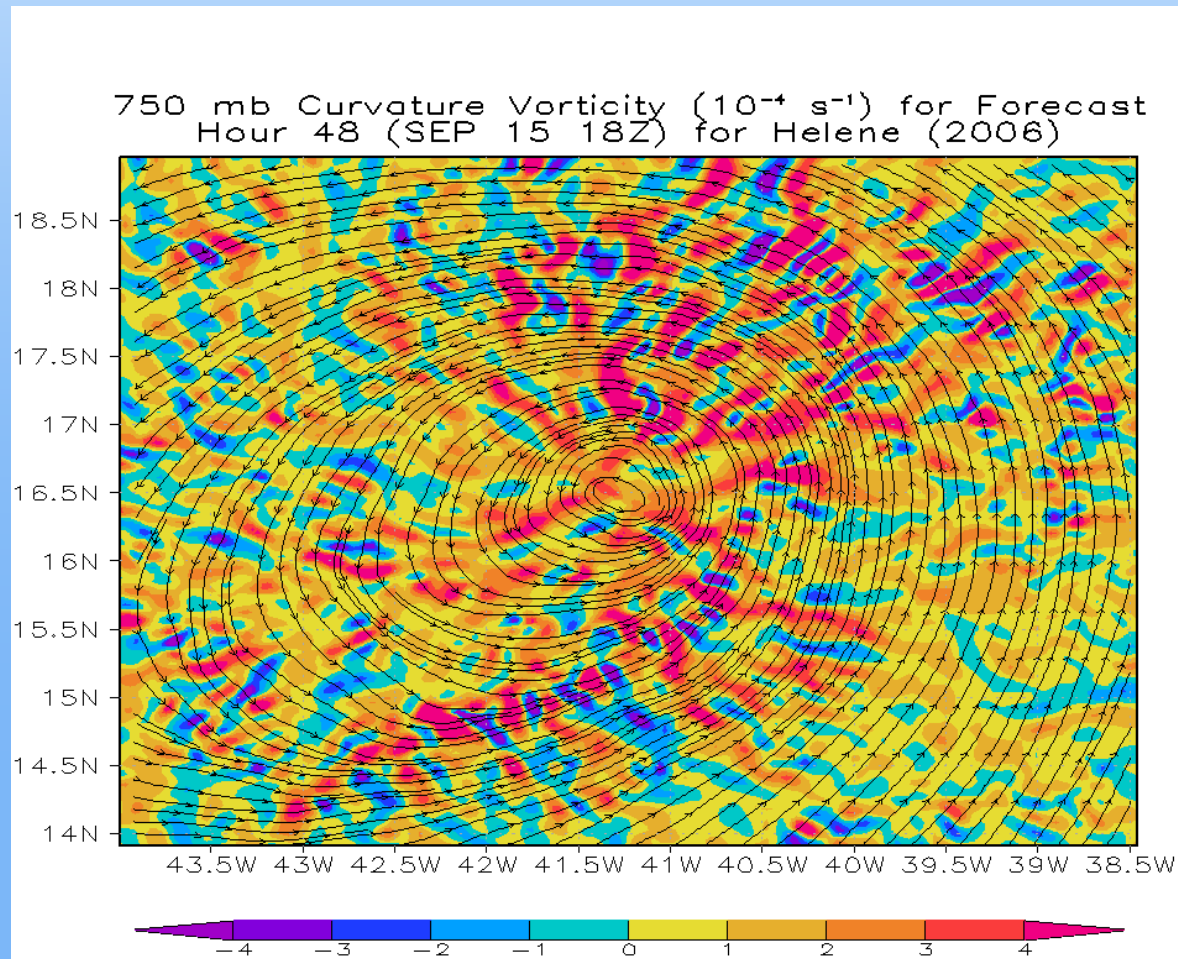
# Accumulated Shear to Curvature for MM5 Run for NAMMA Wave #3

- Magnitude of conversions are smaller
- Curvature vorticity does increase, but no corresponding decrease in shear vorticity



# Curvature Vorticity and Shear Vorticity Plots

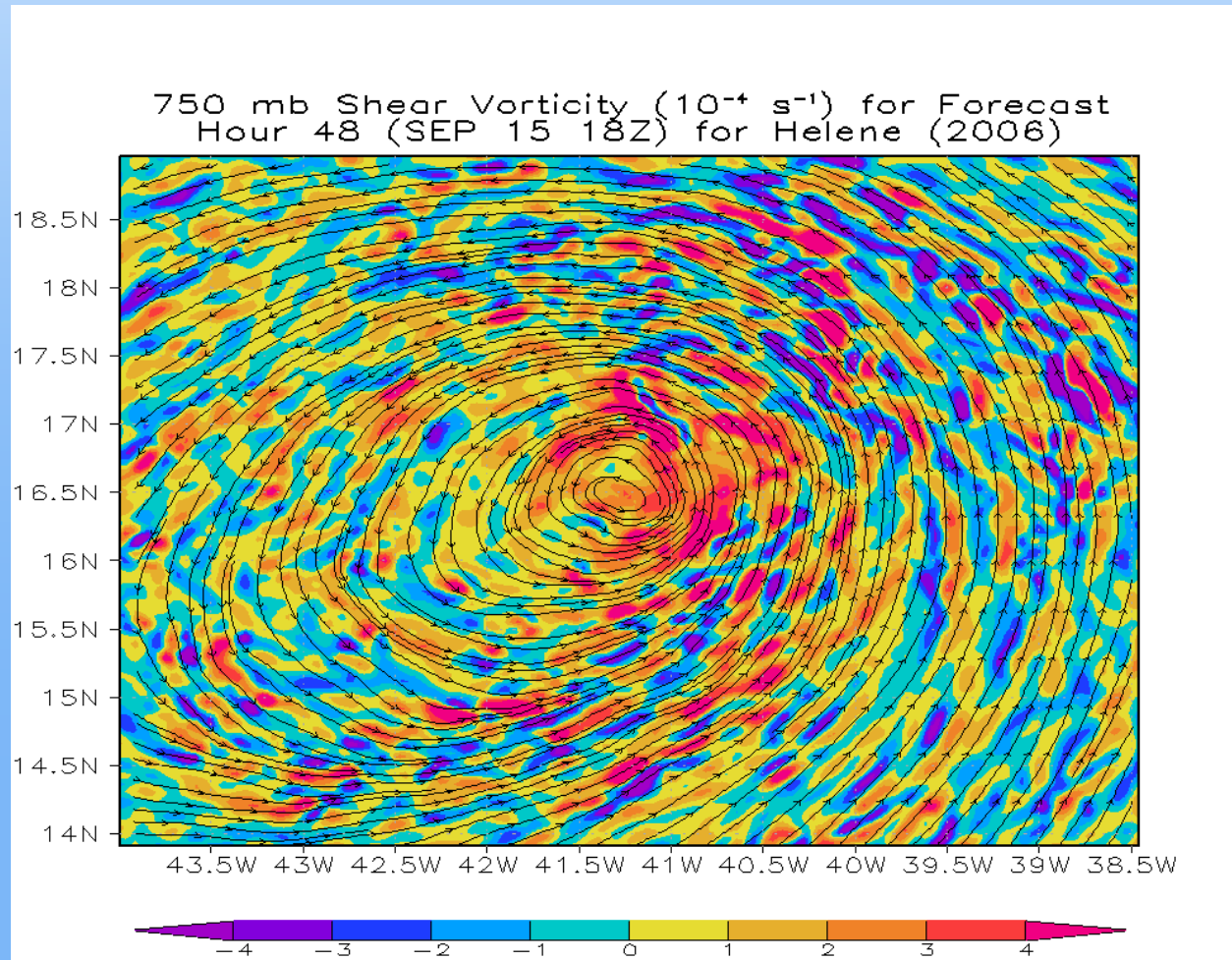
## ■ Curvature Vorticity normal to flow





# Curvature Vorticity and Shear Vorticity Plots

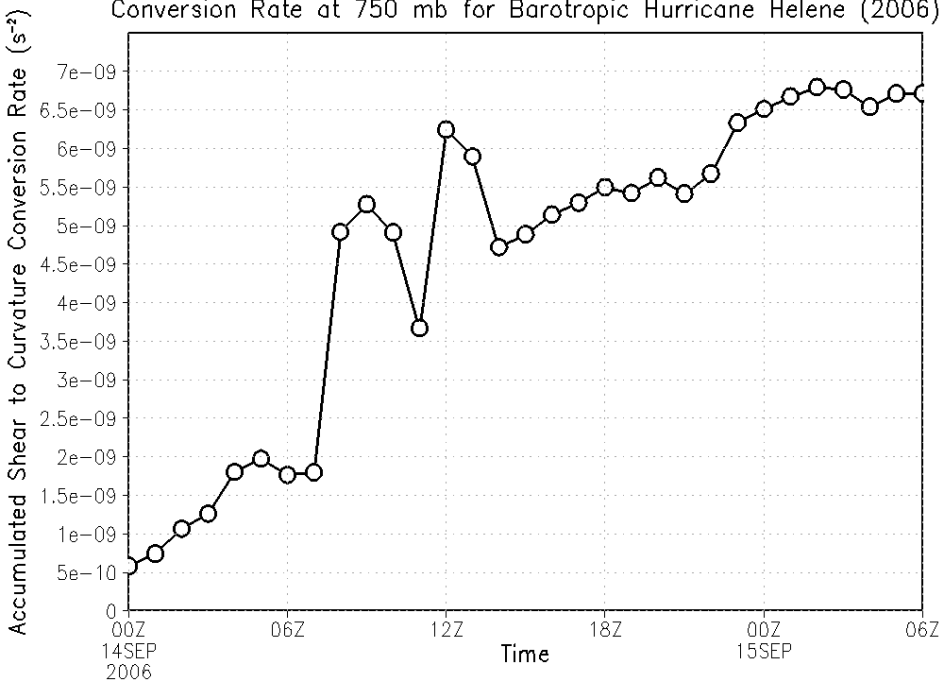
## ■ Shear Vorticity parallel to flow



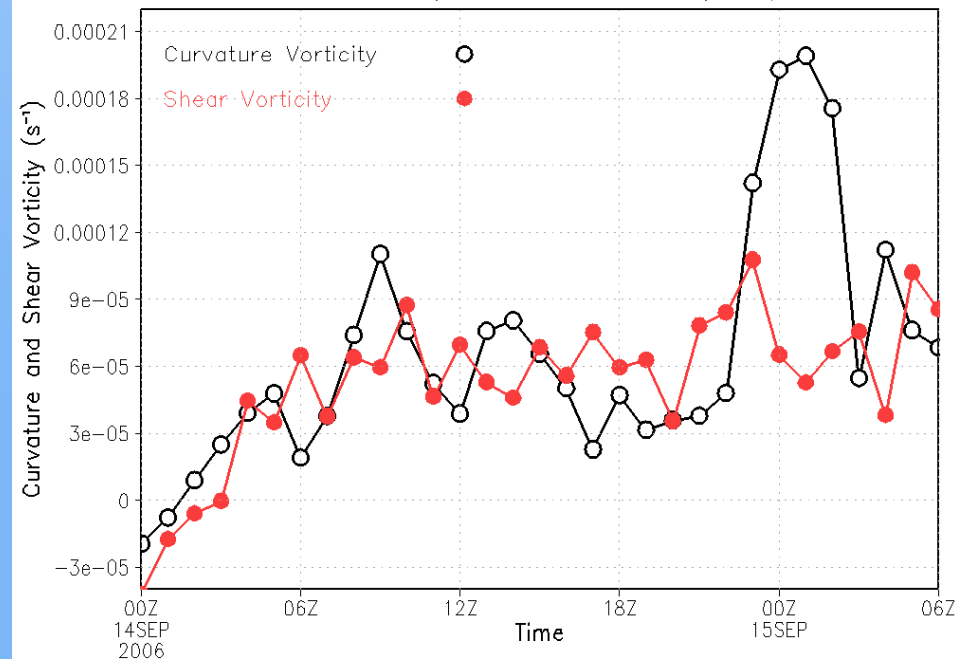
# Barotropic Model Results

- Consistent increase in amount of shear vorticity being converted to curvature vorticity
- Signal from shear vorticity and curvature vorticity budgets is more ambiguous

Box Averaged Accumulated Shear Vorticity to Curvature Vorticity Conversion Rate at 750 mb for Barotropic Hurricane Helene (2006)



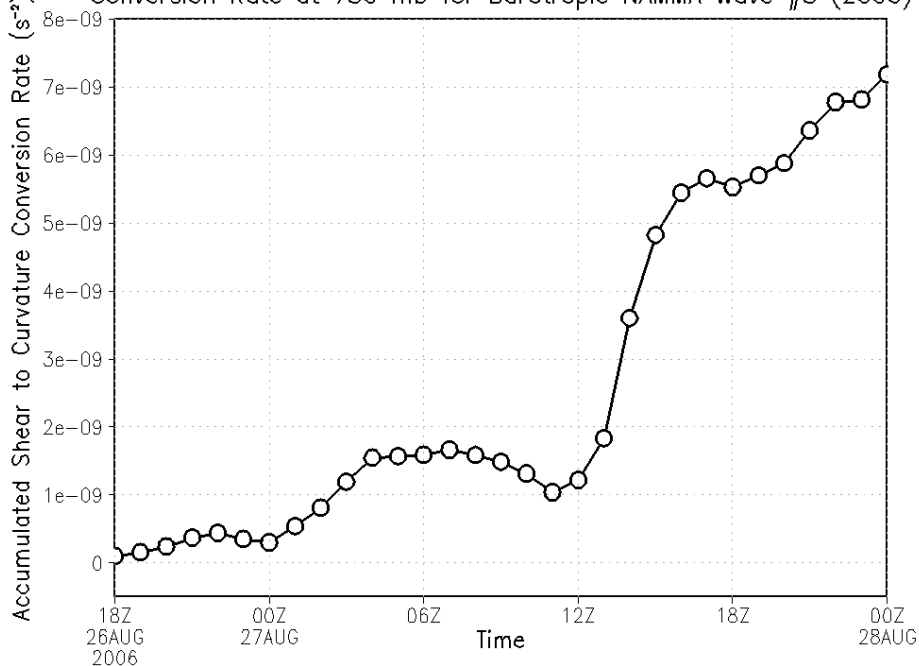
Box Averaged Curvature and Shear Vorticity at 750 mb for Barotropic Hurricane Helene (2006)



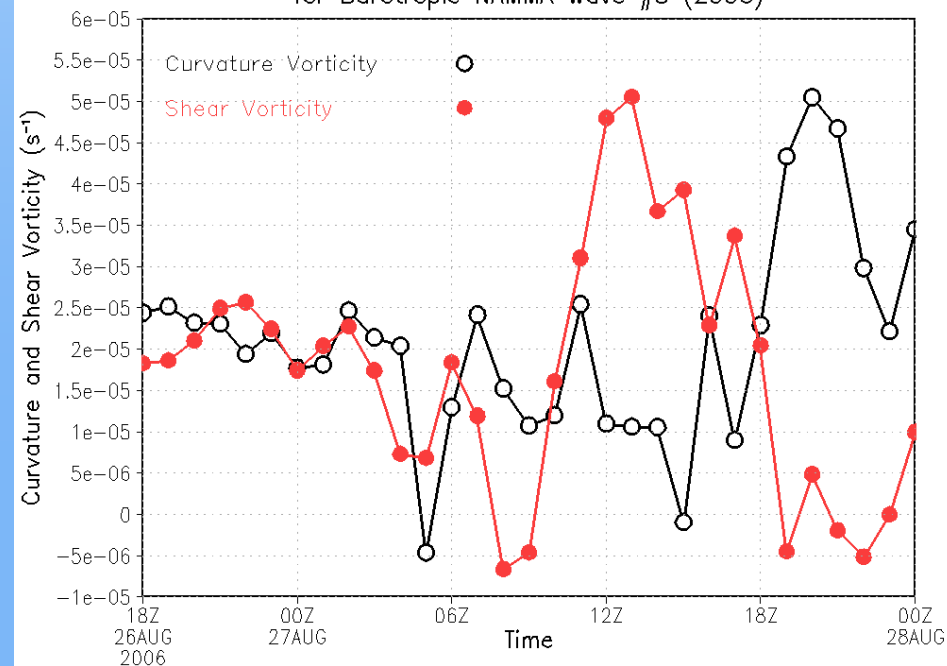
# Barotropic Model Results

- Shear vorticity being converted to curvature vorticity, but ambiguous response in shear vorticity and curvature vorticity budgets

Box Averaged Accumulated Shear Vorticity to Curvature Vorticity Conversion Rate at 750 mb for Barotropic NAMMA Wave #3 (2006)



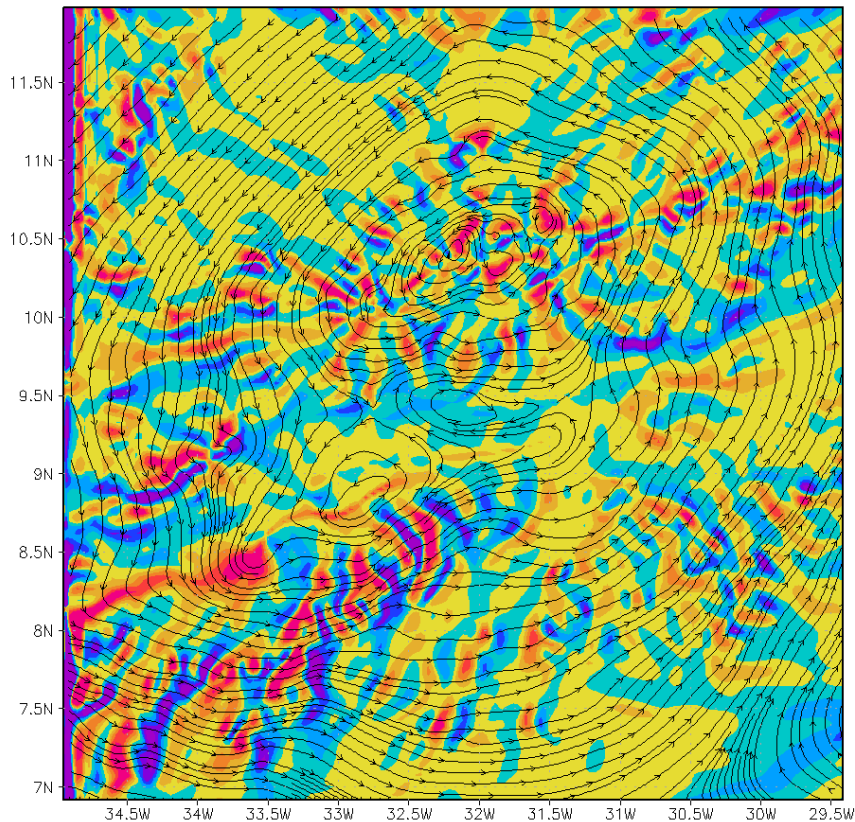
Box Averaged Curvature and Shear Vorticity at 750 mb for Barotropic NAMMA Wave #3 (2006)



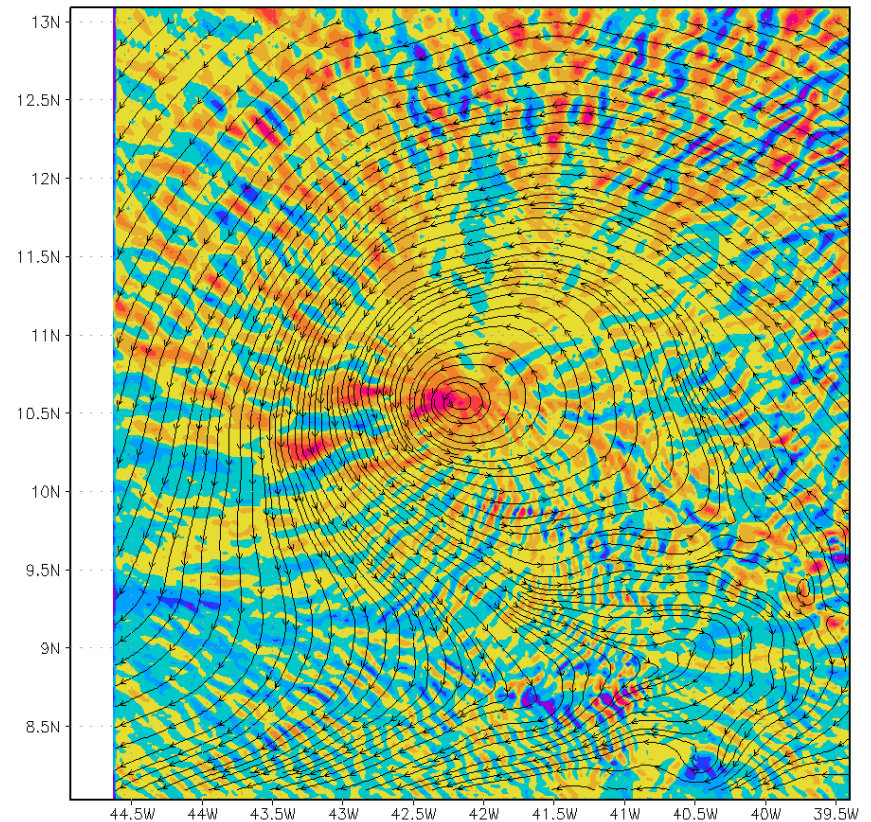
# Barotropic Model Results: Curvature

## Vorticity

750 mb Curvature Vorticity ( $10^{-4} \text{ s}^{-1}$ ) for Forecast Hour 0 (SEP 14 00Z) for Helene (2006)

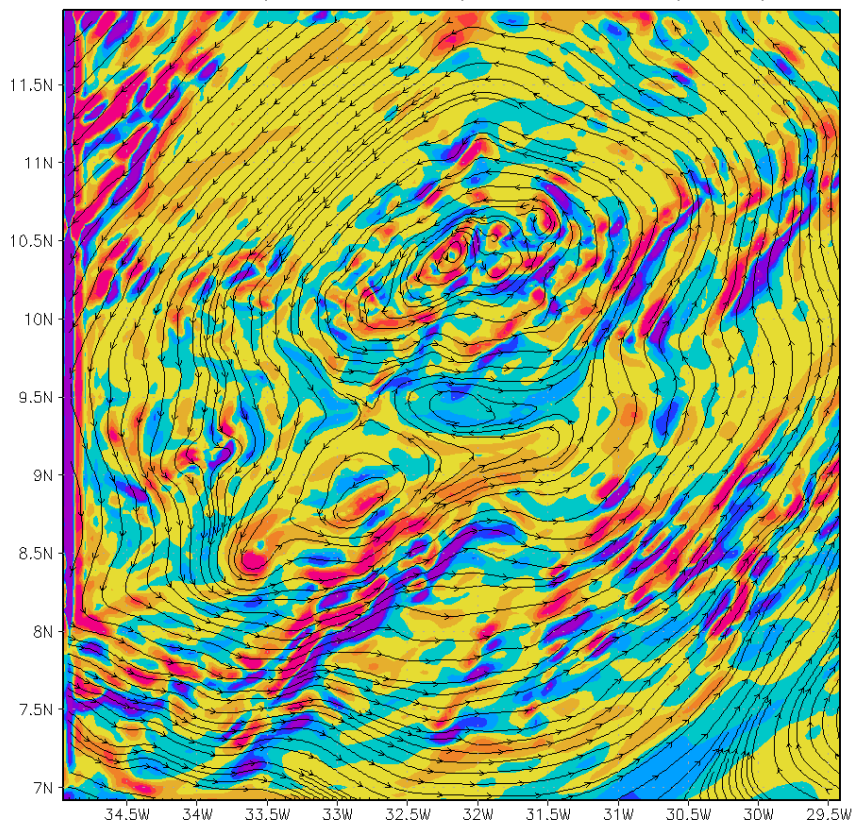


750 mb Curvature Vorticity ( $10^{-4} \text{ s}^{-1}$ ) for Forecast Hour 24 (SEP 15 00Z) for Helene (2006)

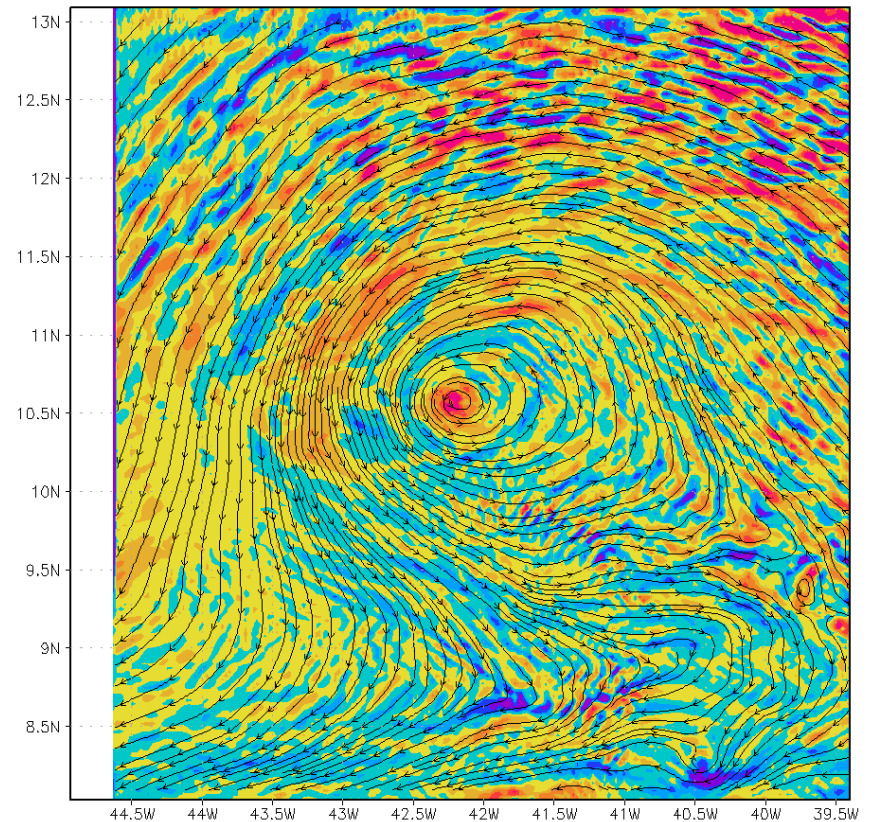


# Barotropic Model Results: Shear Vorticity

750 mb Shear Vorticity ( $10^{-4} \text{ s}^{-1}$ ) for Forecast Hour 0 (SEP 14 00Z) for Helene (2006)



750 mb Shear Vorticity ( $10^{-4} \text{ s}^{-1}$ ) for Forecast Hour 24 (SEP 15 00Z) for Helene (2006)



# Conclusions

- While MM5 hints that shear vorticity to curvature vorticity conversions are important for accounting for curvature vorticity, results from barotropic model are not definitive
  - No difference between developing and non-developing cases in terms of shear vorticity and curvature vorticity conversions
  - Response among vorticities in barotropic model runs not as clear
- Spatial structure of curvature vorticity and shear vorticity similar for MM5 and barotropic model  
→ can be explained using barotropic dynamics

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