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6 **Assimilation of Radar Radial Velocity Data with the WRF Ensemble-**  
7 **3DVAR Hybrid System for the Prediction of Hurricane Ike (2008)**  
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## Abstract

An enhanced version of the hybrid ensemble-3DVAR data assimilation system for the WRF model is applied to the assimilation of radial velocity ( $V_r$ ) data from two coastal WSR-88D radars for the prediction of Hurricane Ike (2008) before and during its landfall. In this hybrid system, flow-dependent ensemble covariance is incorporated into the variational cost function using the extended control variable method. The analysis ensemble is generated by updating each forecast ensemble member with perturbed radar observations using the hybrid scheme itself. The  $V_r$  data are assimilated every 30 minutes for 3 hours immediately after Ike entered the coverage of the two coastal radars.

The hybrid method produces temperature increments showing rainband structures and positive increments in the vortex core region, and a warm core throughout the hurricane depth in the final analysis. In contrast, the 3DVAR produces much weaker and smoother increments with negative values at the vortex center at lower levels. Wind forecasts from the hybrid analyses fit the observed radial velocity better than that from 3DVAR, and the 3-h accumulated precipitation forecasts from the hybrid are also more skillful. The track forecast is slightly improved by the hybrid method and slightly degraded by the 3DVAR compared to the forecast from the GFS analysis. All experiments assimilating the radar data show much improved intensity analyses and forecasts compared to the experiment without assimilating radar data. The better forecast of the hybrid indicates that the hybrid method produces dynamically more consistent state estimations. Little benefit of including the tuned static component of background error covariance in the hybrid is found.

61 **1. Introduction**

62 Tropical cyclones (TCs) are among the most costly forms of natural disaster (Pielke et al.  
63 2008). An accurate TC forecast will require not only a numerical model to realistically simulate  
64 both the TC itself and its environment, but also a data assimilation (DA) system that can  
65 effectively use the observations to accurately estimate the initial TC vortex and the environment  
66 where the TC is embedded in.

67 To address the TC initialization issue, many previous studies adopted the vortex  
68 relocation and/or bogussing (e.g., Liu et al. 2000; Kurihara et al. 1995; Zou and Xiao 2000)  
69 techniques. While such techniques are non-trivial and have been shown to improve the hurricane  
70 forecast, how to maintain the dynamical and thermo-dynamical coherency of the hurricane and  
71 its environment is probably the biggest challenge with such methods.

72 Recently, several studies have explored the use of ensemble-based DA methods to  
73 initialize hurricane forecasts and have shown great promise (e.g., Torn and Hakim 2009; Zhang  
74 et al. 2009; Li and Liu 2009; Hamill et al. 2011; Wang 2011; Dong and Xue 2011). The key with  
75 ensemble-based DA is the use of an ensemble to estimate the forecast error statistics in a flow-  
76 dependent manner. Therefore, the observation information will be properly weighted and spread  
77 consistent with the background hurricane forecasts; and perhaps more importantly, the ensemble  
78 covariance can realistically infer the flow-dependent cross-variable error statistics and therefore  
79 update state variables not directly observed in a dynamically and thermodynamically consistent  
80 manner.

81 One candidate in ensemble-based DA is the hybrid ensemble-variational DA method. It  
82 has been proposed (e.g., Hamill and Snyder 2000; Lorenc 2003; Etherton and Bishop 2004;  
83 Zupanski 2005; Wang et al. 2007b, 2008a; Wang 2010), implemented and tested with real

84 numerical weather prediction (NWP) models and real data recently (e.g., Buehner 2005; Wang et  
85 al. 2008b; Buehner et al. 2010ab; Wang 2011; Wang et al. 2011; Whitaker et al. 2011; Kleist et  
86 al. 2011). Compared to a standard variational method (VAR) that typically uses static  
87 background error covariance, ensemble covariance is incorporated into the VAR framework to  
88 provide a flow-dependent estimate of the background error covariance and the ensemble can be  
89 generated by a version of the ensemble Kalman filter (EnKF). Recent studies have suggested that  
90 the hybrid DA systems may represent the “best of both worlds” by combining the best aspects of  
91 the variational and EnKF systems (e.g., Wang et al. 2007a, 2008ab, 2009; Zhang et al. 2009;  
92 Buehner et al. 2010ab; Wang 2010). While preliminary tests of the hybrid DA system with real  
93 NWP models and data have shown great potential of the method for non-TC forecasts (e.g.,  
94 Wang et al. 2008b; Buehner et al. 2010ab) and for forecasts of TC tracks (e.g., Wang 2011;  
95 Whitaker et al. 2011), to the author’s best knowledge, to date there is no published study  
96 applying hybrid DA method to the assimilation of radar data at a convection-allowing resolution  
97 for TC predictions. This study serves as a pilot study applying the hybrid ensemble-3DVAR  
98 system developed for the WRF model (Wang et al. 2008a) to explore its potential for  
99 assimilating radar observation for hurricane forecasts. As a first step of such study, we focus on  
100 assimilating radar radial velocity data.

101 More specifically, this study applies and explores the WRF ensemble-3DVAR hybrid  
102 system to the assimilation of coastal WSR-88D radar radial velocity data for the prediction of  
103 Hurricane Ike (2008) (Fig. 1). Ike is the third most destructive landfalling hurricane in the  
104 recorded history of United States. Previous studies (e.g., Zhao and Xue 2009) have shown  
105 significant impact of the radar data for this case using ARPS 3DVAR/cloud analysis package.  
106 The remainder of this paper is organized as follows: Section 2 presents the methodology and

107 section 3 discusses the experiment design. The experiment results are discussed in Section 4  
108 while the final section summarizes the main conclusions of this study.

## 109 **2. Methodology**

### 110 *a. The hybrid ensemble-3DVAR scheme*

111 A diagram of the hybrid DA system is shown in Fig. 2. Similar to Hamill and Snyder  
112 (2000), the following four steps are repeated for each DA cycle: 1. Perform K (K is the ensemble  
113 size) number of ensemble forecasts to generate background forecast fields at the time of analysis;  
114 2. Calculate ensemble forecast perturbations to be used by the hybrid cost function for flow-  
115 dependent covariance by subtracting ensemble mean from each member; 3. Generate K  
116 independent sets of perturbed observations by adding random perturbations to the observations;  
117 4. Obtain the analysis increment for each ensemble member through minimization of the hybrid  
118 cost function using one set of perturbed observations. Steps 1 through 4 are repeated for each of  
119 the follow-on cycles, with the ensemble analyses providing initial conditions for step 1. In step 3,  
120 the random perturbations added to the observations are drawn from a Gaussian distribution with  
121 a mean of zero and a standard deviation of the observation error. This is analogous to the  
122 ‘perturbed observation method’ employed in the classic ensemble Kalman filter (Evensen 2003).  
123 In the original work of Wang et al. (2008a) testing the hybrid WRF DA system, the ensemble  
124 transform Kalman filter (ETKF) was used to update forecast perturbations.

125 A brief review on the extended control variable method for incorporating ensemble  
126 covariance into a WRF 3DVAR framework is given here. For detailed discussions, readers are  
127 referred to Wang et al. (2007b, 2008a).

128 For state vector  $\mathbf{x}$ , the analysis increment of the hybrid scheme,  $\mathbf{x}'$ , is the sum of two  
129 terms,

130 
$$\mathbf{x}' = \mathbf{x}'_1 + \sum_{k=1}^K (\mathbf{a}_k \circ \mathbf{x}_k^e). \quad (1)$$

131 The first term  $\mathbf{x}'_1$  in Eq. (1) is the increment associated with WRF 3DVAR static background  
 132 covariance and the second term is the increment associated with flow-dependent covariance.  
 133 Here,  $\mathbf{a}_k$  is the extended control variable as defined by Lorenc (2003),  $\mathbf{x}_k^e$  is the  $k^{\text{th}}$  ensemble  
 134 perturbation state vector. The symbol ‘o’ denotes the Schur product (element by element  
 135 product) of the vectors  $\mathbf{a}_k$  and  $\mathbf{x}_k^e$ .

136 The cost function for WRF ensemble-3DVAR hybrid is

137 
$$J(\mathbf{x}'_1, \mathbf{a}) = \beta_1 J_b + \beta_2 J_e + J_o,$$

138 
$$= \beta_1 \frac{1}{2} (\mathbf{x}'_1)^T \mathbf{B}^{-1} (\mathbf{x}'_1) + \beta_2 \frac{1}{2} (\mathbf{a})^T \mathbf{A}^{-1} (\mathbf{a}) + \frac{1}{2} (\mathbf{y}^{o'} - \mathbf{H}\mathbf{x}')^T \mathbf{R}^{-1} (\mathbf{y}^{o'} - \mathbf{H}\mathbf{x}'). \quad (2)$$

139  $J_b$  is the traditional WRF 3DVAR background term associated with the static covariance  $\mathbf{B}$  and  
 140  $J_e$  is the hybrid term associated with flow-dependent covariance.  $\mathbf{a}$  is defined as  
 141  $\mathbf{a}^T = (\mathbf{a}_1^T, \mathbf{a}_2^T, \dots, \mathbf{a}_K^T)$ .  $J_o$  is the observation term associated with observation error covariance  $\mathbf{R}$ .  
 142 The innovation vector  $\mathbf{y}^{o'}$  is defined as,  $\mathbf{y}^{o'} = \mathbf{y}^o - \mathbf{H}(\mathbf{x}^b)$ , where  $\mathbf{y}^o$  is the observation vector,  $\mathbf{x}^b$  is  
 143 the background forecast state vector, and  $\mathbf{H}$  is the linearized observation operator.

144 The weights of the static covariance and flow-dependent covariance are determined by  
 145 factors  $\beta_1$  and  $\beta_2$  according to relationship

146 
$$\frac{1}{\beta_1} + \frac{1}{\beta_2} = 1, \quad (3)$$

147 which conserves the total variance.

148 As described in Wang et al. (2008a), the ensemble covariance localization, denoted as  $\mathbf{A}$ ,  
 149 has horizontal and vertical components. In this study, both the horizontal and vertical  
 150 localization are applied. Specifically, the horizontal localization is modeled by a recursive filter

151 transform as in Wang et al. 2008a. The vertical localization is implemented by transforming the  
152 extended control variable  $\mathbf{a}$  in Eq. (2) with empirical orthogonal functions (EOFs). The  
153 correlation matrix, denoted as Cov, from which the EOFs is derived, follows

$$154 \quad \text{Cov}(k_1, k_2) = \exp\left(-\frac{d^2}{L^2}\right), \quad (4)$$

155 where  $d$  is the distance between model levels  $k_1$  and  $k_2$  and  $L$  is the vertical localization radius.  
156 Existing EOF codes in the WRF 3DVAR for modeling the vertical static error covariance is used  
157 for the vertical ensemble covariance localization purpose.

### 158 **3. Experimental design**

#### 159 *a. The WRF model configuration*

160 The Advanced Research WRF (ARW) model version 3 is used in this study (Skamarock  
161 et al. 2008). The model is compressible, three-dimensional, non-hydrostatic, discretized on a  
162 Arakawa C grid with terrain-following mass-based sigma coordinate levels. In this study, the  
163 WRF model is configured with 401x401 horizontal grid points at 5-km grid spacing (Fig. 1), and  
164 41 vertical levels with the model top at 100 hPa. The WRF single-moment six-class scheme  
165 (Hong et al. 2004) is chosen for the explicit microphysics processes. Since the grid resolution  
166 may not fully resolve the hurricane convective features, the Grell-Devenyi cumulus  
167 parameterization scheme (Grell; Devenyi 2002) is included. Other physics parameterizations  
168 schemes used include the Yonsei University (YSU) (Noh et al. 2003) scheme for planetary  
169 boundary layer parameterization, the 5-layer thermal diffusion model for land surface processes  
170 (Skamarock et al. 2008), the Rapid Radiative Transfer Model (RRTM) longwave (Mlawer et al.  
171 1997), and the MM5 shortwave (Dudhia 1989) radiation parameterization.

172 *b. The radar data processing*

173 The radial velocity data from coastal WSR-88D radars at Houston, Texas (KHGX) and  
174 Lake Charles, Louisiana (KLCH) are processed using a modified version of the Four  
175 Dimensional Dealiasing Algorithm (James; Houze 2001). The algorithm was originally designed  
176 for Doppler radars in European Alps. The modified algorithm by this study is capable of reading  
177 level-II WSR-88D data and dealiasing the radial velocities.

178 To dealias radial velocity data, the following steps are performed: First, a wind profile is  
179 created based on model background, rawinsonde, or wind profiler data. The background radial  
180 velocity in radar observation space is calculated from the wind profile, assuming the wind is  
181 horizontally homogeneous. Second, the WSR-88D radial velocity is compared with the  
182 background radial velocity for a gross check. In this step, aliased radial velocity that needs to be  
183 corrected is identified. Third, at each elevation angle, spatial dealiasing is performed. The aliased  
184 velocity  $V_a$  will be recovered by factored Nyquist velocity  $V_n$ ,

$$185 \quad V_d = V_a + 2NV_n, \quad (5)$$

186 where  $N$  is a positive or negative integer whose sign and value are determined by a gate-to-gate  
187 shear threshold of  $0.4V_n$  (James and Houze 2001). After dealiasing is finished, the radial velocity  
188 interpolated to the Cartesian coordinates is thinned to 10 km spacing horizontally and 500 meter  
189 vertically.

190 Figure 3 shows the processed radial velocity at  $0.5^\circ$  elevation angle for KHGX (Fig. 3a)  
191 and KLCH (Fig. 3b) at 0000 UTC 13 September 2008. These two radars complement each other  
192 by providing scans that are approximately the right angle at the location of Ike's eye. KHGX  
193 covers almost all of Ike's eye and eye wall. The outbound radial velocity on the left side of the  
194 eye and inbound radial velocity on the right side of the eye reflect the circulation of the



195 hurricane. KLCH covers only about half of eye and eye wall. The outbound radial velocity on  
196 the front side of the eye and inbound radial velocity on the back side of the eye also reflect the  
197 circulation of the hurricane.

198 The observation error standard deviation for the radial velocity is set to  $2 \text{ m s}^{-1}$  during the  
199 DA. This error value is similar to the values used in (Dowell; Wicker 2009), (Xu; Gong 2003),  
200 and (Xiao et al. 2009; Xiao et al. 2009).

### 201 *c. The data assimilation setup*

202 This paper presents five experiments denoted as NoDA, 3DVARa, 3DVARb, HybridF,  
203 and HybridH (Table 1). Experiments differ based on what, if any, assimilation system is used for  
204 radar data. The experiments are designed to examine the difference of using flow-dependent  
205 versus static background covariance when assimilating the radar data and the impact of DA on  
206 the subsequent forecast.

207 The NoDA experiment did not assimilate any radar data, instead the WRF model initial  
208 condition at 0300 UTC 13 September 2008 simply comes from the  $1^\circ \times 1^\circ$  degree NCEP (National  
209 Centers for Environmental Prediction) operational GFS (Global Forecast System) analysis. The  
210 6-hourly GFS analyses also provide the lateral boundary conditions (LBCs).

211 The “3DVARb” experiment assimilated the radar data using the traditional 3DVAR  
212 method where the static background covariance is adopted. The static covariance is generated  
213 and further tuned as followed. The NMC method (Parrish; Derber 1992) was first employed to  
214 generate the static background covariance statistics based on 12-h and 24-h WRF model  
215 forecasts, starting at 00 UTC and 12 UTC every day, during the period from 01 to 15 September  
216 2008. The experiment using the static covariance generated by the above procedure without  
217 further tuning is denoted as 3DVARa. Because the default correlation length scales derived from

218 the NMC method reflects mostly large-scale error structures, their direct use may not be  
219 appropriate for storm-scale radar DA (Liu et al. 2005). The horizontal correlation length scale of  
220 the static covariance is reduced by a factor of 0.3 in experiment 3DVARb and this factor is found  
221 to be optimal through experimentations. The 3DVAR experiments contains three stages (Fig.  
222 4a): (1) a single 6-h spinup forecast initialized from the GFS analysis at 1800 UTC, September  
223 12, to produce an initial first guess at 0000 UTC, September 13 for radar DA cycles; (2)  
224 assimilation of radial velocity data from KHGX and KLCH radars every 30 minutes for 3 hours;  
225 (3) a 21-h deterministic forecast initialized by the analysis at the end of the assimilation cycles in  
226 (2). The WRF model boundary conditions for all three stages are also provided by the  
227 operational GFS analyses at 6 hourly intervals. Experiment 3DVARb serves as a base line for  
228 evaluating the performance of the hybrid method.

229 Experiments HybridF and HybridH are identical except that the different weighting  
230 factors  $\beta_1$  and  $\beta_2$  are used in Eq. (2). For HybridF, the full weight is assigned on the flow-  
231 dependent ensemble covariance (using  $\beta_1 = 0.001$  and  $\beta_2 = 1.001$ ). For HybridH, the static  
232 covariance and the flow-dependent ensemble covariance are equally weighted ( $\beta_1 = 0.5$  and  $\beta_2 =$   
233  $0.5$ ), i.e., only half of the flow-dependent covariance is used, hence the ‘H’ in the name. The  
234 horizontal correlation scale of static covariance in HybridH is also reduced by a factor of 0.3 as  
235 in 3DVARb. Meanwhile, HybridH uses the same flow dependent covariance localization as  
236 HybridF, which will be discussed in detail in section 4.a.

237 Each of the hybrid experiments, HybridF and HybridH, has 40 ensemble members.  
238 Similar to the 3DVAR experiments, the hybrid experiments have three stages (Fig. 4b): (1) 6-h  
239 ensemble forecasts to spin up a first guess ensemble and provide flow-dependent covariance at  
240 the beginning of the radar DA cycles. The initial and boundary conditions for each member are

241 the GFS analysis plus correlated random perturbations following Torn et al. (2006) and Wang et  
242 al. (2008a,b); (2) assimilation of perturbed radial velocity data from KHGX and KLCH radars  
243 every 30 minutes for 3 hours by variationally minimizing the hybrid cost function, according to  
244 the description given in the previous section (see also Fig. 2); (3) a 21-h deterministic forecast  
245 initialized from the ensemble mean analysis at the end of the DA cycles in (2). To generate the  
246 random perturbations in (1), the random-cv facility in the WRF 3DVAR system is employed  
247 (Barker et al. 2004). First, a random control variable vector is created with a normal distribution  
248 having a zero mean and unit standard deviation. Then the perturbation control variable vector is  
249 transformed to the model space to obtain perturbations to the model state variables including the  
250 horizontal wind components, pressure, potential temperature, and mixing ratio of water vapor.  
251 The perturbation standard deviations are roughly  $1.9 \text{ m s}^{-1}$  for the horizontal wind components,  
252  $0.6 \text{ K}$  for temperature,  $0.3 \text{ hPa}$  for model pressure perturbation, and  $0.9 \text{ g kg}^{-1}$  for water vapor  
253 mixing ratio and these values are based on the NMC-method-derived background error statistics.

254 The relaxation method of Zhang et al. (2004) is used for ensemble covariance inflation.  
255 The inflated ensemble perturbation  $\mathbf{x}'_{\text{new}}$  is a weighted average of prior perturbation  $\mathbf{x}'_{\text{f}}$  and  
256 posterior perturbation  $\mathbf{x}'_{\text{a}}$ ,  $\mathbf{x}'_{\text{new}} = (1 - b) \mathbf{x}'_{\text{f}} + b \mathbf{x}'_{\text{a}}$ , the relaxation coefficient, denoted as  $b$ , is set  
257 to 0.5.

#### 258 **4. Results and discussion**

259 The analysis increment of the first DA cycle, the cycling process, the final analysis fields,  
260 and the deterministic forecasting results will be presented and discussed in this section. The  
261 subsection organization roughly follows the experiment flow charts in Fig. 4.

262 *a. Single observation test for vertical localization*

263 Before complete DA experiments are performed, the vertical covariance localization in  
264 the hybrid scheme is tested by assimilating a single radial velocity observation. Figure 5 shows  
265 the wind speed increment produced by HybridF analyzing a single radial velocity observation  
266 located 3176 m above sea level at 0000 UTC 13 September 2008. The innovation (i.e., the  
267 observed radial velocity minus forecast ensemble mean valid at 0000 UTC 13 September) for  
268 this observation is  $-38.63 \text{ m s}^{-1}$ . Without the vertical localization, nonzero increment reaches the  
269 top of the model with relatively noisy increments at the upper levels (Fig. 5a). The horizontal and  
270 vertical localization radii of 60 and 3 km, respectively, are used in hybrid experiment HybridF  
271 (and in HybridH), and were arrived at after a range of localization scales was tested. Figure 5b  
272 shows that with such localizations, the analysis increment is limited to the region within a radius  
273 from the observation location, mitigating negative effects of unreliable distant covariance that  
274 are unavoidable with a limited-sized ensemble. This single observation test verifies the  
275 correctness of our implementation of the vertical localization.

276 *b. Wind increments*

277 To see the differences in analyzing the radar data using flow-dependent and static  
278 covariances, the analysis increments from the 3DVAR and hybrid experiments after the first  
279 analysis time are compared. We first look at the wind increments and will look at indirectly  
280 related cross-variable increments in the next subsection.

281 Figure 6 shows the wind analysis increments at 850 hPa, at 0000 UTC 13 September  
282 2008, the time of first analysis for 3DVARa, 3DVARb, HybridF, and HybridH. The increment in  
283 3DVARa using the default NMC-method-derived static covariance shows cyclonic and anti-  
284 cyclonic increment patterns of rather large scales (Fig. 6a); the cyclonic increment circulation is

285 centered almost 2 degrees off the observation hurricane center to the southsoutheast, while at the  
286 hurricane center location the wind increment is mostly easterly. To the north the increment  
287 circulation shows an anti-cyclonic pattern. Such cyclonic and anti-cyclonic increments are also  
288 found in a previous studies assimilating radar radial velocity data using WRF 3DVAR (e.g., Xiao  
289 et al. 2007), but are clearly unrealistic, and do not reflect the fact that a strong vortex exists  
290 where the background strongly underestimate the strength of the vortex. The default background  
291 error covariance derived from the NMC method is unaware of the hurricane vortex and its spatial  
292 correlation scales mostly reflect synoptic scale error structures. The net result is the  
293 inappropriately large amount of smoothing of the radar data in the data dense region and  
294 inappropriately large spreading of the information outside the data coverage region. The radar  
295 data, being collected at high spatial resolution, should be analyzed using much smaller spatial  
296 correlation scales. This had been pointed out in Liu et al. (2005) and the use of smaller  
297 correlation scales for radar data is a common practice in the ARPS 3DVAR system (e.g.,  
298 Schenkman et al. 2011).

299 In 3DVARb, the default horizontal spatial correlation scale is reduced by a factor of 0.3.  
300 The resulting wind increment now shows a more or less symmetric cyclonic pattern around the  
301 observed center of Ike (Fig. 6b). Compared with 3DVARa, the large increments are more limited  
302 to the region of vortex in 3DVARb, and the increment is consistent with the inbound and  
303 outbound radial velocity couplets associated with the hurricane vortex as observed by KHGX  
304 and KLCH radars (Fig. 3). Such results are more realistic.

305 In HybridF with full weight given to the flow-dependent covariance, the wind increment  
306 also shows a cyclonic pattern centered around the eye of Ike (Fig. 6c), but the increment  
307 circulation is less axisymmetric, reflecting the contribution of spatially inhomogeneous flow-

308 dependent covariance. When equal weights are placed on the ensemble covariance and static  
309 covariance in HybridH, the wind increments show a pattern that is close to that of 3DVARb, but  
310 the increment magnitude is between those of the HybridF and 3DVARb (Fig. 6d).

311 *c. Temperature increments*

312 Because radar radial velocity is the only data type assimilated in this study, any  
313 increment in temperature is the result of balance relationship applied (if any) and/or due to cross-  
314 covariance in the background error. Figure 7 shows the 850 hPa temperature increments for  
315 3DVARb, HybridF, and HybridH after assimilating radial velocity data for the first cycle. For  
316 3DVARb, negative temperature increments are found in the vortex region, and the magnitude is  
317 largest near the hurricane center (Fig. 7a). Physically, enhanced hurricane vortex circulation  
318 should be accompanied by warming of the vortex core region, to give a warmer core vortex;  
319 hence the 3DVAR temperature increment is inconsistent with expected hurricane structures. The  
320 negative increment is expected of the 3DVAR, because the increment is obtained through a  
321 balance relationship between temperature and wind and this relationship reflects the thermal  
322 wind relation. More specifically, the ‘balanced temperature’ increment  $T_b$  at a vertical level  $k$ , in  
323 WRF 3DVAR is related to the stream function  $\psi$  by a regression relation,  $T_b(k) = \sum_l G(l,k) \psi(l)$ ,  
324 where  $G$  is the regression coefficient and the summation is over the vertical index  $l$ . Such a  
325 regression relation derived using the NMC-method generally reflects hydrostatic, geostrophic,  
326 and thermal wind relations (Barker et al. 2004). A colder core at 850 hPa is consistent with an  
327 enhanced cyclonic circulation at the 700 hPa seen in Fig. 6. Note that at this distance, the lowest  
328 radar beams do not reach below 850 hPa, hence the enhancement of wind is larger above 850  
329 hPa. Therefore the cyclonic wind increment increases with height in the lower atmosphere. We  
330 note that negative temperature increment is also seen in the low-level eye region of analyzed

331 hurricanes in previous studies using Airborne Doppler radar data and WRF 3DVAR (e.g., Xiao  
332 et al. 2009)

333 Different from 3DVAR, the temperature increment obtained in HybridF shows positive  
334 increments in the eye region (Fig. 7b) and spiral patterns in the eye wall and outer rainband  
335 regions. Such much more realistic structures are the result of temperature-wind cross covariances  
336 derived from the ensemble, which have knowledge of the vortex as a tropical cyclone. In  
337 addition, the magnitude of the temperature increments in HybridF is an order of magnitude larger  
338 than that of 3DVARb; the temperature increment in the 3DAR analysis of Xiao et al. (2009) for  
339 Hurricane Jeanne (2004) was also weak, reflecting the relative weak thermal wind relationship in  
340 3DVAR.

341 As the wind increment, the temperature increment from HybridH is in-between those of  
342 HybridF and 3DVARb (Fig. 7c). The magnitude is about half that of HybridF. The structure of  
343 the increment resembles that of HybridF more but the eye region has negative instead of positive  
344 increments. From this aspect, HybridH is poorer than HybridF.

#### 345 *d. Innovation statistics for Vr and minimum sea level pressure in DA cycles*

346 The behaviors of 3DVARb, HybridH, and HybridF are further compared by examining  
347 the fit of their analyses and forecasts to Vr observations during the DA cycles. The fit is defined  
348 as the root mean square difference (RMSD) between the model state and observations, after the  
349 model state is converted to the observed quantities; and such difference is also called observation  
350 innovation. Figure 8 shows the RMSDs for Vr and minimum sea level pressure (MSLP) from  
351 HybridH, HybridF and 3DVARb. Vr data of both KHGX and KLCH are used in the innovation  
352 calculation and for the hybrid, the ensemble mean is used. In all three experiments, the RMSD  
353 for Vr is reduced significantly by the analysis within each cycle and the largest reduction occurs

354 in the first analysis cycle at 0000 UTC when the observation innovations are the greatest. In later  
355 cycles, the innovations for the analyses remain roughly between 2.5 and 3.5 m s<sup>-1</sup>, which is  
356 reasonable given the 2 m s<sup>-1</sup> expected observation error. The 30-minute forecasts following each  
357 analysis generally increase the Vr innovation by about 2 m s<sup>-1</sup>, reaching 4-5 m s<sup>-1</sup> levels. In  
358 general, HybridH produces analyses that fit Vr observations tightest while HybridF the least and  
359 3DVARb is in-between. Similar is true of the 30-minute forecasts. It is interesting that the  
360 innovations for HybridH are not generally in-between HybridF and 3DVARb, as we saw earlier  
361 for the wind and temperature increment fields. We note that such results are possible and can  
362 occur, for example, when the observed value is closer to the value of HybridH, that may be in-  
363 between the values of HybridF and 3DVAR. The observation innovation statistics can help us to  
364 see if the DA system is doing about the right things, but being ‘verification’ against the same set  
365 of observations that is also used in the DA, it cannot really tell us the true quality of the analyses.  
366 True measures of the analysis quality require verifications against independent observations or  
367 verification of subsequent forecasts, which will be presented later.

368 Figure 8b shows the fit of the analysis and forecast MSLPs to the best track data from the  
369 National Hurricane Center. The best track MSLP is more or less constant during this 3 hour  
370 period, being at about 952 hPa. At the beginning of DA cycling (0000 UTC 13 September), the  
371 MSLP is about 23 hPa higher than the best track estimate. The reduction of MSLP by HybridF  
372 is slightly larger than those of HybridH and 3DVARb in the first analysis. Later on, the reduction  
373 by 3DVARb is minimal. Significant reduction in MSLP occurred at 0200 UTC for HybridF, and  
374 at 0100 and 0130 UTC for HybridH while in all other cycles the reduction by analysis is  
375 minimal. Most of the reduction in MSLP in all cases are actually achieved through adjustment  
376 during the forecasting process, with more than 15 hPa reduction achieved during the first



377 analysis cycle between 0000 and 0030 UTC. This is not surprising because wind is the only  
378 parameter directly measured, and pressure analysis increments are only achieved through balance  
379 relationships and/or cross covariance, which are apparently weak.

380 We note in general, the MSLP decreases faster in the forecast stages in the hybrid  
381 experiments than in 3DVARb. This is consistent with the fact that the hybrid method tends to  
382 build a warmer vortex core, and warmer temperature tends to induce a lower surface pressure  
383 due to hydrostatic balance. A stronger vortex circulation will also induce lower central pressure  
384 due to cyclostrophic balance. During the final 3 cycles, there is clearly over-deepening of the  
385 central pressure in HybridH in the forecast stages, resulting in a fall of MSLP that is about 5.5  
386 hPa too low compared to best track. The final analysis MSLP in HybridF is about 2.0 hPa too  
387 low, which should be within the uncertainty range of MSLP best track data.

388 Overall, errors in the maximum surface wind (MSW) and MSLP are greatly reduced after  
389 assimilating radar data in all DA experiments. At 0300 UTC 13 September, the end of the DA  
390 cycles, the best track MSW and MSLP are  $47.5 \text{ m s}^{-1}$  and 951 hPa respectively. For 3DVARb,  
391 HybridF, and HybridH, after assimilating radar radial wind, the MSW errors are 1, 0.8, and 2.7  
392  $\text{m s}^{-1}$  and the MSLP errors are 0.2, 1.9, and 5.6 hPa, respectively. In contrast, for NoDA  
393 experiment without assimilating radar data, the MSW error is  $9 \text{ m s}^{-1}$  and MSLP error is 29 hPa.

#### 394 *e. The analyzed hurricane structures*

395 We examine next the structure of the hurricane at the end of the DA cycles by plotting  
396 fields at the surface and in vertical cross sections through the analyzed hurricane center. Figure 9  
397 shows the analyzed mean sea level pressure and surface wind vectors for NoDA, 3DVARb,  
398 HybridF and HybridH. Compared with NoDA (Fig. 9a), the analyzed vortex circulations are  
399 stronger and the minimum sea level pressure is much lower in 3DVARb, HybridF, and HybridH

400 (Fig. 9b-d). The low level flow also shows convergence towards the eye wall; such primary  
401 hurricane circulations (Willoughby 1990) are captured well by the assimilation of radar radial  
402 velocity data.

403 Figure 10 shows the vertical cross sections of horizontal wind speed and potential  
404 temperature for all four experiments. The locations of cross sections are through the analyzed  
405 hurricane center and the maximum wind speed as indicated by the thick lines in Fig. 9. The  
406 hurricane eye is much wider and the intensity is much weaker in NoDA than in the three radar  
407 DA experiments. Given the inner eye pressure deficit, the warm core should extend through the  
408 depth of the troposphere based on the hydrostatic approximation (Haurwitz 1935). Compared  
409 with the hybrid experiments, 3DVARb shows an unrealistic weak cold core structure at the lower  
410 levels. With the downward extruding potential temperature contours in HybridF and HybridH  
411 throughout the depth of the plotted domain (Fig. 10c, d), the warm core structure is clear.

412 The warm core structure is seen even more clearly in the vertical cross sections of  
413 horizontal temperature anomaly, which is the deviation from the mean at the pressure levels (Fig.  
414 11). The temperature anomaly in NoDA is very small (less than 2 K, Fig. 11a) while that in  
415 3DVARb, HybridF and HybridH exceeds 8 K, with the maximum anomaly found between 300  
416 and 500 hPa levels (Fig. 11b-d). Such temperature anomalies are expected in hurricanes at  
417 similar intensities. Zhu et al. (2004) obtained a maximum anomaly of about 8 K in an 84-h  
418 forecast of Hurricane Bonnie (1988) with a MSLP of about 955 hPa. In observational studies, the  
419 strength of hurricane warm core has been shown to negatively correlate with MSLP (Halverson  
420 et al. 2006; Hawkins; Imbembo 1976).

421 The near-zero or negative temperature anomaly below 700 hPa is clear in Fig. 11b for  
422 3DVARb. This is related to the negative 3DVARb temperature increment discussed earlier. In

423 HybridF and HybridH, the positive anomaly extends to the surface (Fig. 11c and 11d). In the  
424 latter two, the maximum anomaly is found to be at the inner edge of hurricane eye wall at about  
425 400 hPa, which should be associated with the eye wall warming (LaSeur and Hawkins 1963;  
426 Holland 1997).

427 *f. The track and intensity forecasts*

428 To further evaluate the quality of analyses produced by different DA methods,  
429 deterministic forecasts initialized from the (ensemble mean in the hybrid cases) analyses at 0300  
430 UTC 13 September, the end of the DA cycles, are launched. The track forecasts are compared in  
431 Figure 12a. The center of hurricane is defined as the location of MSLP. The initial track errors at  
432 0300 UTC are less than 20 km for all four experiments. By 0000 UTC 14 September, the track  
433 errors are 98, 117, 84, 64 km for NoDA, 3DVARb, HybridF and HybridH respectively. The  
434 mean track errors based on the hurricane positions at 6-h interval during the period from 0300  
435 UTC 13 to 0000 UTC 14 September are 41, 57, 41, and 34 km for NoDA, 3DVARb, HybridF,  
436 and HybridH respectively. Given that our DA experiments do not include environmental  
437 observations, the main effect on the track should come from the changes to the structure and  
438 intensity of the analyzed hurricane.

439 Figure 12b shows the intensity forecasts in terms of MSLP, together with the best track  
440 MSLP. At 0300 UTC 13 September, the MSLP errors are 28, 0.2, 2.0, and 5.5 hPa for NoDA,  
441 3DVARb, HybridF and HybridH respectively. NoDA has the largest MSLP error throughout the  
442 forecast. The MSLP error in 3DVARb is smaller at the initial time, but becomes larger than those  
443 of HybridF and HybridH at the later forecast times. Overall, the forecast MSLP in the two hybrid  
444 experiments is closer to the best track MSLP than that of 3DVARb. None of the forecasts  
445 capture the slight deepening during the first 3 hours of forecast.

446 *g. Verification of forecasts against Vr observations*

447         The wind forecasts are further verified against observed radar radial velocity data. Figure  
448 13 shows the root mean squared errors (RMSEs, strictly it is RMSD because observations also  
449 contain error) of forecast against observed Vr for 3DVARb, HybridF and HybridH. Compared to  
450 the best track estimation of wind speed, the radar Vr observations are more reliable. At the initial  
451 time of 0300 UTC, the RMSE of  $3.5 \text{ m s}^{-1}$  from HybridF is slightly larger than those from  
452 HybridH ( $2.6 \text{ m s}^{-1}$ ) and 3DVARb ( $2.8 \text{ m s}^{-1}$ ). After the first hour, the HybridF wind forecast fits  
453 the observed radial wind best, especially after 6 hours of forecast where the error in 3DVARb  
454 grows much faster and reaching  $14.8 \text{ m s}^{-1}$  compared to the  $8\text{-}9 \text{ m s}^{-1}$  in the hybrid cases. The  
455 much faster error growth in 3DVARb, even though at the initial time its fit to Vr observations is  
456 comparable to that of HybridH and better than HybridF, suggests that other model fields in the  
457 3DVARb analysis are dynamically less consistent with the wind field than in the hybrid cases.  
458 The slight better forecast in HybridF than in HybridH at 6 hours suggests the fully flow-  
459 dependent covariance during the assimilation cycles is beneficial.

460 *h. Evaluation of rainfall forecasts*

461         Rainfall forecasts are evaluated by calculating equitable threat scores (ETSs) of 3-h  
462 accumulated precipitation against NCEP Stage IV precipitation analyses (Fig. 14). For the  
463 thresholds of 5, 10, and 25 mm/3 hr and all forecast lead times, the hybrid experiments have  
464 higher ETSs than 3DVARb. Furthermore, the improvement of the hybrid over 3DVARb  
465 increases with precipitation threshold, indicating again the superior quality of the hybrid DA  
466 method. In addition, HybridF has slightly higher ETS scores than HybridH for most times and  
467 thresholds. The ETS of the hybrid experiments is higher than the NoDA for larger threshold and  
468 longer forecast lead times. By further looking at the precipitation patterns, it is found that the

469 precipitation forecasts of HybridF more closely match the observed convective spiral band  
470 patterns in the inner core region while 3DVARb produces too much precipitation in the southeast  
471 quadrant in the outer band region (the region is within the reflectivity coverage of coastal radars,  
472 from which the Stage IV precipitation is estimated, c.f. Fig. 1) and the radius of the inner core  
473 eye wall appears larger than observed (Fig. 15). In comparison, the precipitation pattern from  
474 NoDA case is poorer than the DA experiments especially for inner rain bands.

## 475 **5. Summary and conclusions**

476         In this study, the WRF hybrid ensemble-3DVAR data assimilation (DA) system (Wang et  
477 al. 2008a,b) is applied for the first time to the assimilation of radial velocity data for a landfalling  
478 hurricane. More specifically, radial velocity data from two operational WSR-88D radars along  
479 the Gulf of Mexico coast are assimilated over a three-hour period for Hurricane Ike (2008) after  
480 it moved into the ranges of the two radar, using an enhanced version of the WRF hybrid DA  
481 system. Different from Wang et al. (2008a,b) that employed an ensemble transformation Kalman  
482 filter to generate the analysis ensemble, we employ in this study the ‘perturbed observation’  
483 method used in Hamill and Snyder (2000), which corresponds to the stochastic approach used in  
484 the classic stochastic ensemble Kalman filters (Burgers et al. 1998; Houtekamer and Mitchell  
485 1998; Evensen, 2003). Further, we applied vertical localization based on empirical orthogonal  
486 functions while continuing to use recursive filters for horizontal localization for the flow-  
487 dependent ensemble-estimated background error covariance. The flow-dependent ensemble  
488 covariance is incorporated into the 3D variational framework by using the extended control  
489 variable method.

490         The radial velocity data are assimilated every 30 minutes over a 3 hour period. Results  
491 mainly from five experiments are presented. A forecast experiment without assimilating any

492 radar data is first carried out to serve as a baseline against which the radar-assimilating  
493 experiments are compared; this forecast experiment (NoDA) started directly from the operational  
494 GFS analysis at 0300 UTC 13 September 2008, which contained too weak a hurricane vortex.  
495 The four radar DA experiments used the WRF 3DVAR using the static covariance derived from  
496 the NMC method (3DVARa), the WRF 3DVAR using further tuned static covariance  
497 (3DVARb), the hybrid DA system with purely flow-dependent background covariance  
498 (HybridF), as well as half static and half flow-dependent covariance (HybridH), respectively. In  
499 the tuned 3DVAR experiment (3DVARb) as well as HybridH, the horizontal spatial correlation  
500 scale in the static covariance derived from the NMC-method is reduced by a factor of 0.3 to  
501 produce much more realistic wind increments than the default scale (in 3DVARa). The results of  
502 analyses and forecasts from the five experiments are inter-compared and verified against best  
503 track data, radar wind measurements and precipitation data. The main conclusions are  
504 summarized in the following.

505       (1) When using the default background error covariance derived from the NMC method  
506 (experiment 3DVARa), WRF 3DVAR produces unrealistic wind increments from radial velocity  
507 ( $V_r$ ) data of two Doppler radars having good coverage of the hurricane vortex. With a reduced  
508 spatial covariance correlation scale (in 3DVARb), the wind increments properly reflect the  
509 hurricane primary circulation.

510       (2) The largest wind increments are obtained in the first few analysis cycles. The  
511 increments of the hybrid scheme with full flow-dependent covariance (in HybridF) produce a  
512 less axisymmetric increment circulation than 3DVARb and HybridH.

513       (3) HybridF produces the most realistic temperature increments with positive values at  
514 the hurricane center, corresponding to the warm core structure, while 3DVARb produces much

515 weaker and smoother temperature increments that are negative at the center of hurricane. At the  
516 end of assimilation cycles, negative temperature anomalies are found below 700 hPa in the eye  
517 region of 3DVARb analysis while the hybrid analyses show deep warm core structures.

518 (4) All three DA experiments are able to create analyses that fit the Vr data well, and the  
519 error reduction by analysis is the largest in the first analysis cycle. The analysis fit to Vr  
520 observations is the closest in HybridH and the least close in HybridF in general during the DA  
521 cycles. Most of the minimum sea level pressure (MSLP) reduction is achieved through model  
522 adjustment during the forecast step of the assimilation cycles, and the MSLP is within 2.5 hPa of  
523 the best track value after 4 analysis cycles of 30 minute interval. HybridH over-analyzes the final  
524 MSLP by about 5.6 hPa while those of 3DVARb and HybridF are within 0.2 and 1.9 hPa of the  
525 best track data, respectively.

526 (5) The hybrid experiments improve the Ike track forecast slightly, over the track forecast  
527 by NoDA starting from the GFS analysis. 3DVARb slightly degrades the track forecast. All radar  
528 DA experiments produce MSLP forecasts that are generally within 8 hPa of the best track data,  
529 with 3DVARb predicting the weakest hurricane among the DA experiments. The NoDA  
530 experiment from GFS analysis starts with an error of nearly 30 hPa in MSLP and ends with an  
531 error of a little over 10 hPa when Ike was much weaker after landfall.

532 (6) The most interesting is that the fit of forecast radial velocity to radar observations  
533 during the first 6 hours of forecast is much worse with 3DVARb than with HybridF and  
534 HybridH, having RMSEs of about 14.8, 8.5 and 9.3  $\text{m s}^{-1}$  for the three, respectively, at the 6-hour  
535 forecast, even though the final analysis of 3DVARb fits the observations closer than that of  
536 HybridF (about 2.8 and 3.5  $\text{m s}^{-1}$ , respectively). The forecast results indicate that the overall  
537 quality of hybrid analyses is better than that of 3DVARb, producing more dynamically consistent

538 state estimations that lead to later slower error growth during forecast. The forecast error of  
539 HybridF is slightly lower than that of HybridH starting from hour three. In the absence of  
540 independent observations for verification during the data assimilation period, the quality of an  
541 analysis is best measured by the accuracy of the ensuing forecast.

542 (7) The equitable threat scores (ETSs) for 3-hour accumulated precipitation forecasts in  
543 the hybrid experiments are higher than those of 3DVARb for the thresholds and lead times  
544 considered, and the improvement increases with precipitation threshold, indicating again the  
545 superior quality of the hybrid DA method. Among the hybrid experiments, HybridF produced  
546 slightly better ETSs than HybridH most times.

547 (8) The results of this study also show positive impacts of assimilating radar data for  
548 hurricane initialization, and the hybrid-method-analyzed hurricane has kinematic and  
549 thermodynamic structures that are consistent with tropical cyclone conceptual models.

550 Finally a point worth noting: the inclusion of static background covariance in HybridH  
551 in general did not improve the results over HybridF; i.e., the use of flow-dependent covariance in  
552 full in general gives better results. Earlier studies suggested that the optimal combination of the  
553 static and flow-dependent covariance depends on their relative quality (Hamill and Snyder 2000;  
554 Wang et al. 2007a). Our results suggest that for hurricanes and radar data, there is little benefit of  
555 including static covariance because static covariance is not capable of appropriately reflecting  
556 the mesoscale and convective-scale nature of hurricanes, and because of the dominant scales of  
557 motion that radar data measure.

558 We also note that this study represents the first attempt of applying a variational-  
559 ensemble hybrid data assimilation method to hurricane and radar data assimilation. While the  
560 results are positive and encouraging, more robust conclusions will need to be drawn by testing



561 the method on many more cases. Other observational data should also be assimilated together to  
562 improve the hurricane environment as well. These are topics for future research.

563

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571

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726 **Table Caption**

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728 Table 1. List of experiments

729 **Figure Captions**

730 Fig. 1. The WRF model domain and National Hurricane Center best track positions for Hurricane  
731 Ike (2008) from 1800 UTC 12 to 0000 UTC 14 September 2008. Also indicated are the  
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737 containing a different set of perturbations.

738 Fig. 3. The radial velocity (interval of 20 m s<sup>-1</sup>) at 0.5° elevation angle from (a) KHGX and (b)  
739 KLCH WSR-88D radars at 0000 UTC 13 September 2008. Black dot is for NHC best-  
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741 Fig. 4. The flow charts for (a) NoDA experiment, (b) 3DVAR experiments (3DVARa and  
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744 single KHGX radar radial velocity data located at (28.4°N, 93.7°W, 3176 m) with an  
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746 without and (b) with vertical localization at 0000 UTC 13 September 2008.

747 Fig. 6. The 700 hPa wind analysis increments (m s<sup>-1</sup>) for (a) 3DVARa, (b) 3DVARb, (c)  
748 HybridF, and (d) HybridH at 0000 UTC 13 September 2008.

749 Fig. 7. The 850 hPa temperature analysis increments for (a) 3DVARb (at intervals of 0.3 K),  
750 (b) HybridF (at intervals of 0.7 K), and (c) HybridH (at intervals of 0.3 K), at 0000  
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754 NHC best track estimate, for 3DVARb, HybridF, and HybridH from 0000 to 0300  
755 UTC 13 September 2008.

756 Fig. 9. The analyzed sea level pressure (interval of 5 hPa, solid contours) and the surface  
757 wind vectors ( $\text{m s}^{-1}$ ) for (a) NoDA, (b) 3DVARb, (c) HybridF, and (d) HybridH at  
758 0300 UTC 13 September 2008. The thick solid line indicates the vertical cross section  
759 location in Fig. 10 and Fig. 11.

760 Fig. 10. Vertical cross sections of analyzed horizontal wind speed (interval of  $10 \text{ m s}^{-1}$ ,  
761 shaded) and potential temperature (interval of 5 K, solid contours) for (a) NoDA, (b)  
762 3DVARb, (c) HybridF, and (d) HybridH, at 0300 UTC 13 September 2008.

763 Fig. 11. Vertical cross sections of analyzed temperature anomalies (interval of 2 K) for (a)  
764 NoDA, (b) 3DVARb, (c) HybridF, and (d) HybridH, at 0300 UTC 13 September  
765 2008.

766 Fig. 12. Deterministic forecast hurricane (a) tracks and (b) minimum sea level pressure (hPa)  
767 by NoDA, 3DVARb, HybridF, and HybridH as compared to NHC best track  
768 estimates from 0300 UTC 13 through 0000 UTC 14 September 2008.

769 Fig. 13. Deterministic forecast RMSEs of  $V_r$  ( $\text{m s}^{-1}$ ) by 3DVARb, HybridF, and HybridH  
770 from 0300 to 0900 UTC 13 September 2008.

771 Fig. 14. The equitable threat scores for 3 h accumulated forecast precipitation by NoDA,  
772 3DVARb, HybridF, and HybridH at thresholds (a) 5 mm, (b) 10 mm, and (c) 25 mm,  
773 verified against NCEP Stage-IV precipitation analyses valid at 0600, 0900, 1200, and  
774 1500 UTC 13 September 2008.

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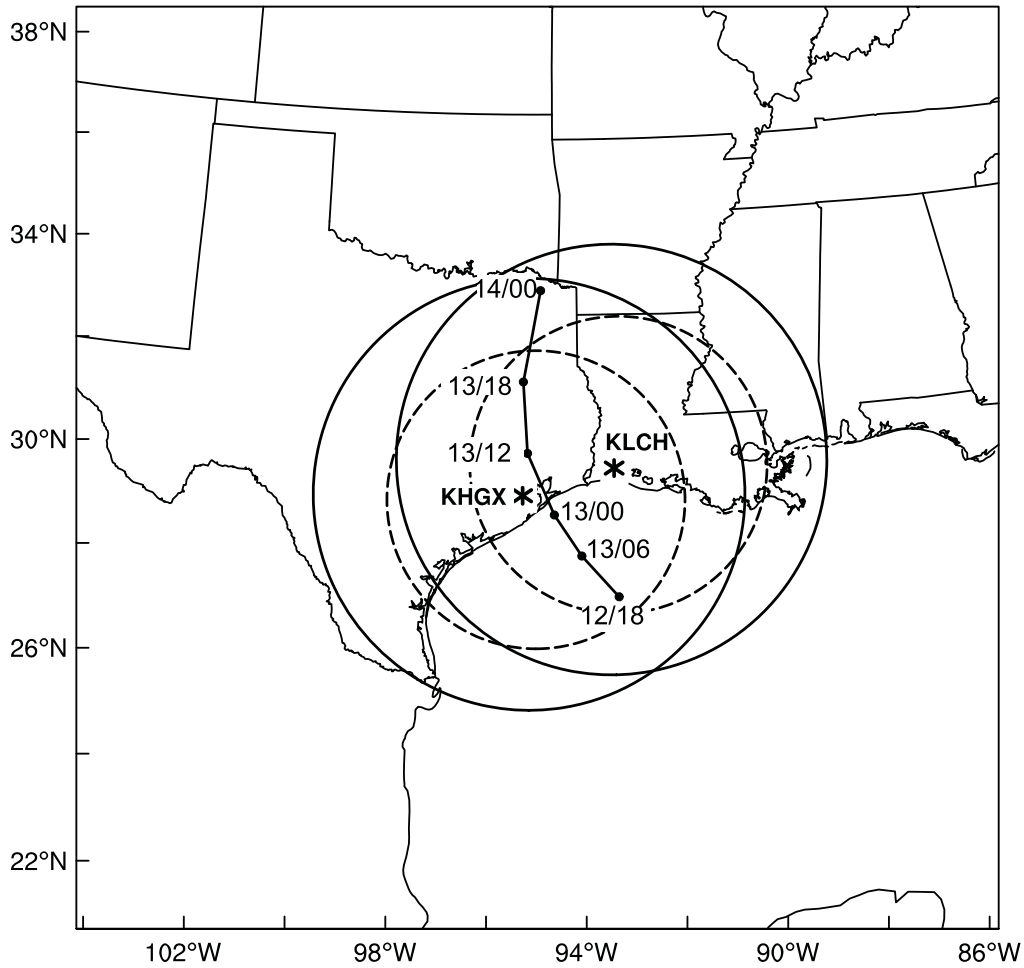
Fig. 15 Three-hour accumulated precipitation (mm) by (1st column) NCEP Stage-IV precipitation analyses, (2nd column) NoDA, (3rd column) 3DVARb, and (4th column) HybridF valid at (top) 0600 and (bottom) 0900 UTC 13 September 2008.

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Table 1. List of experiments

Experiment	Description
NoDA	No radar data assimilation. WRF model initial condition interpolated from NCEP 1°x1° analysis
3DVARa	Radar DA using WRF 3DVAR with static covariance from NMC method
3DVARb	Same as 3DVARa, except the horizontal spatial correlation in the static covariance is multiplied by 0.3.
HybridF	Radar DA using hybrid method with full weight given to flow dependent covariance, with $\beta_1 = 0.001$ and $\beta_2 = 1.001$ in Eq. (1)
HybridH	Hybrid method with equal weight given to static covariance (which is the same as 3DVARb) and flow-dependent covariance, with $\beta_1 = 0.5$ and $\beta_2 = 0.5$ in Eq. (1)

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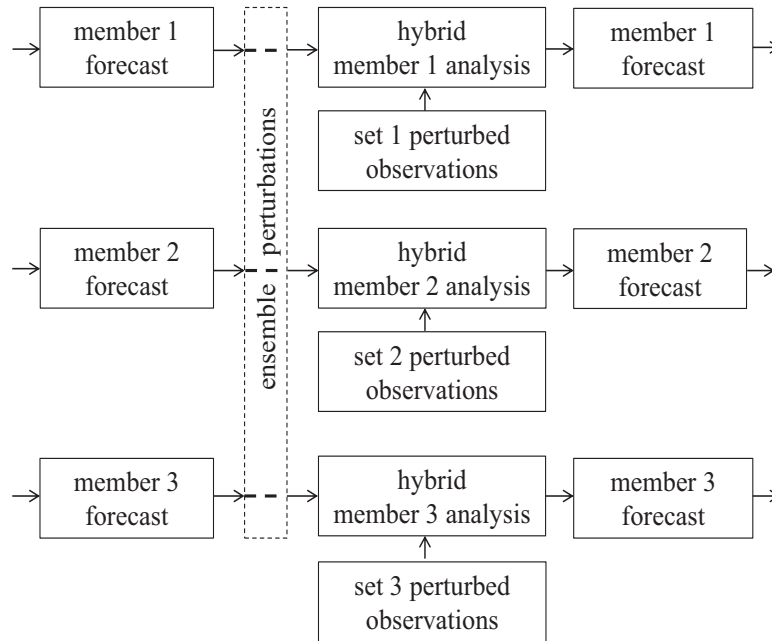
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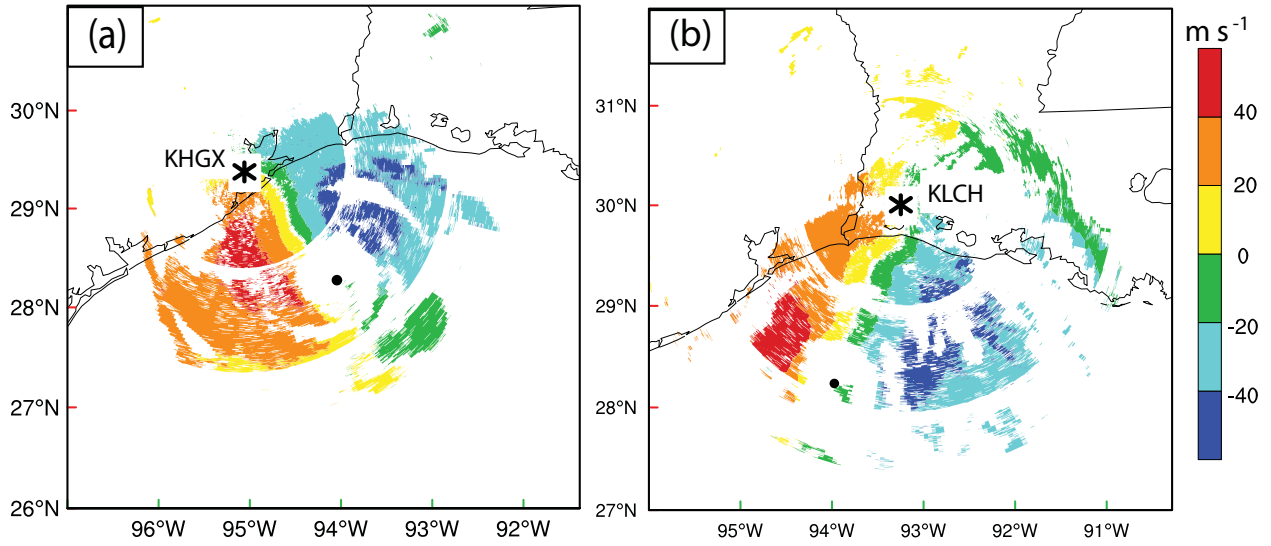
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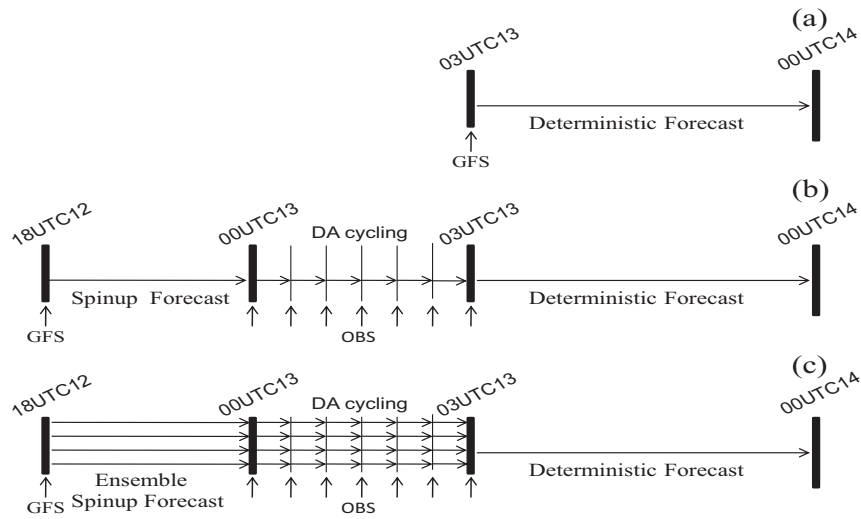
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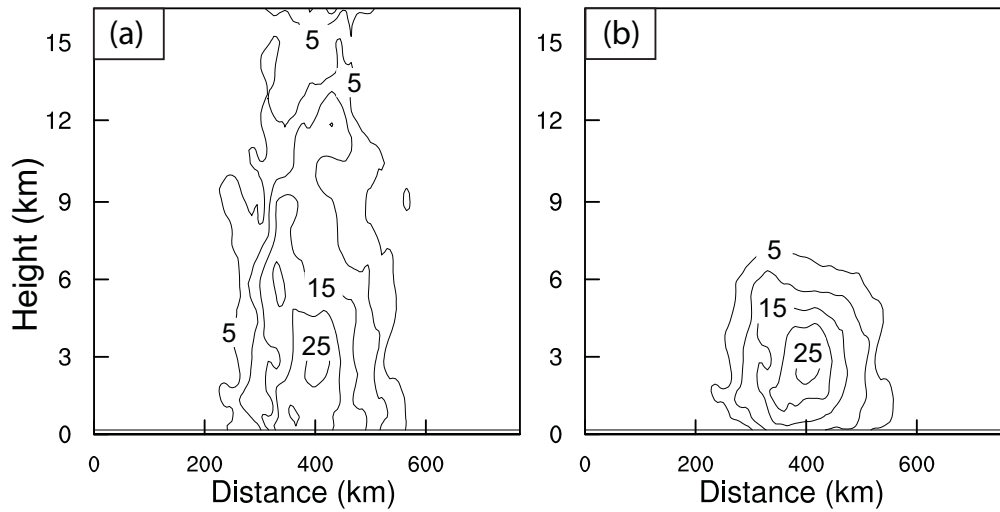


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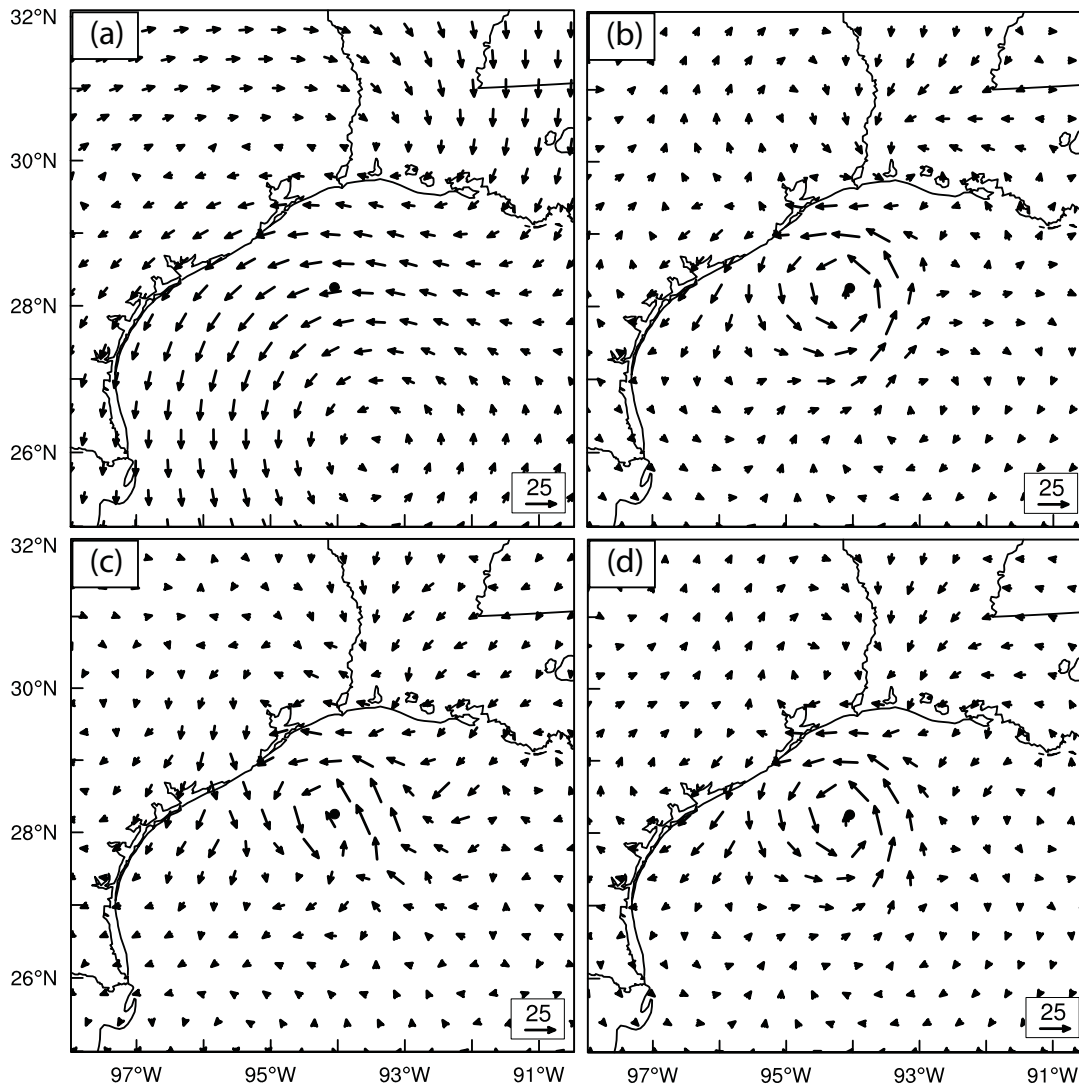
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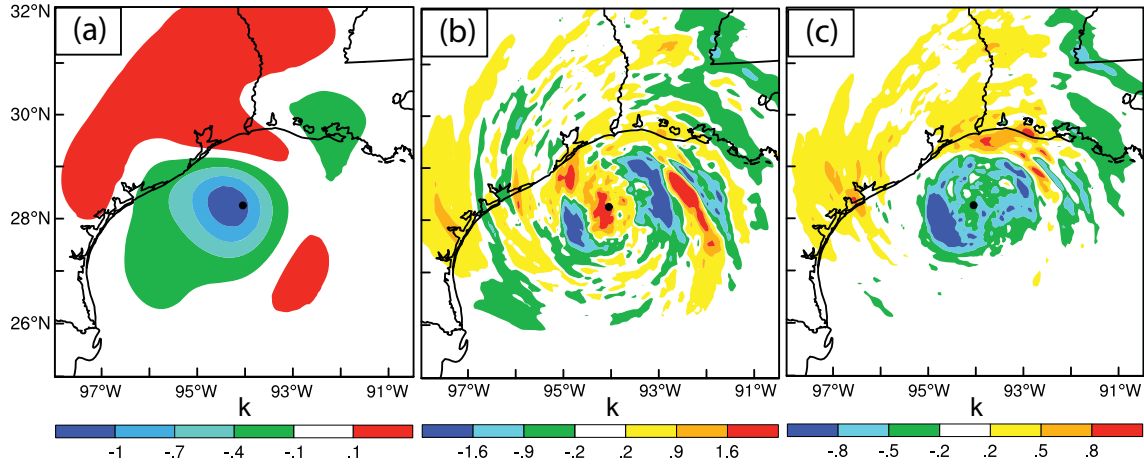
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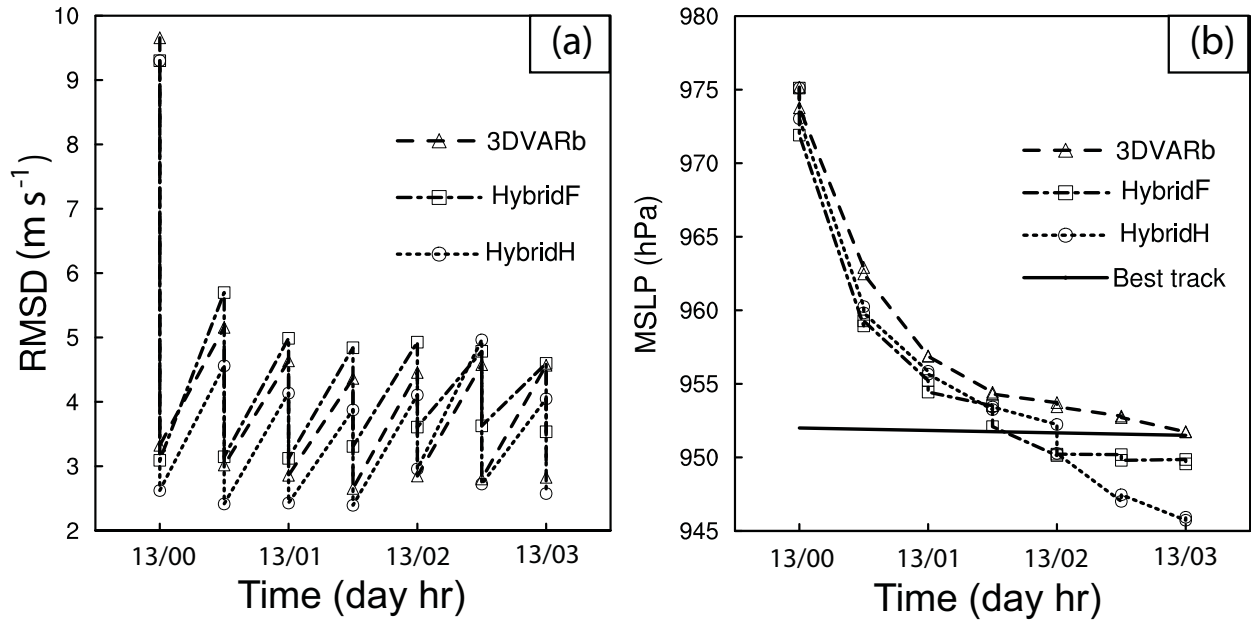


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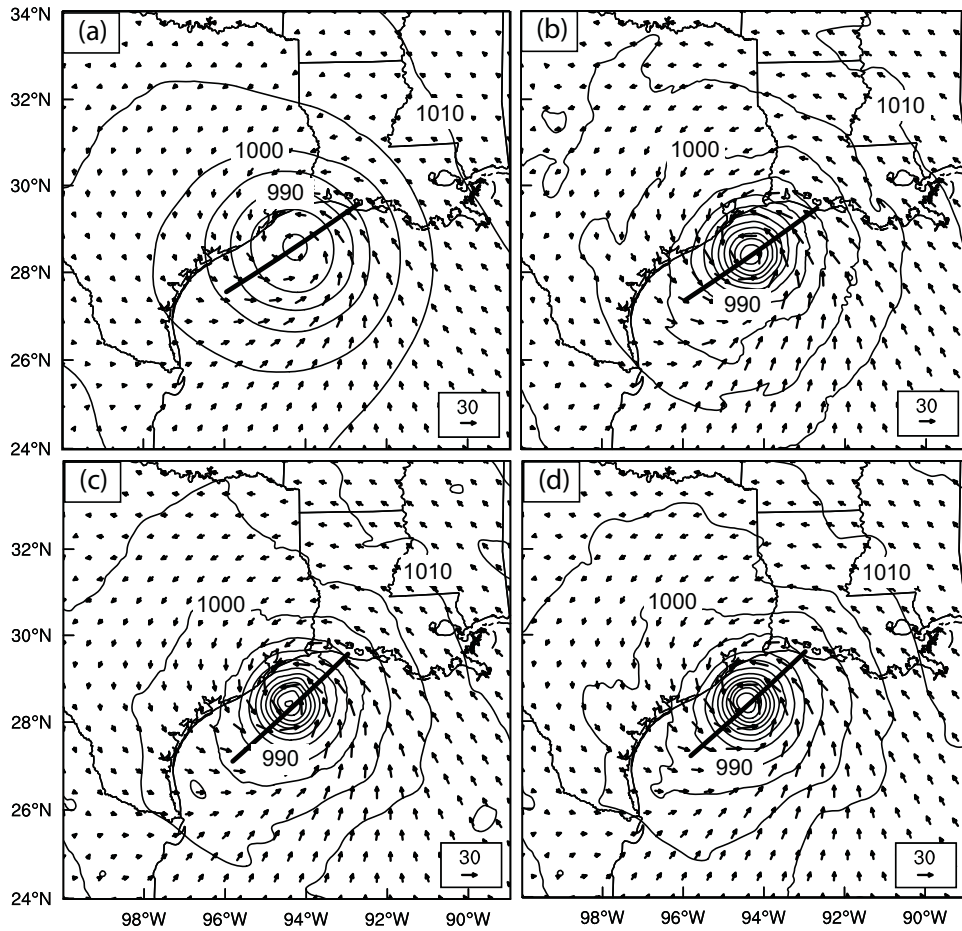


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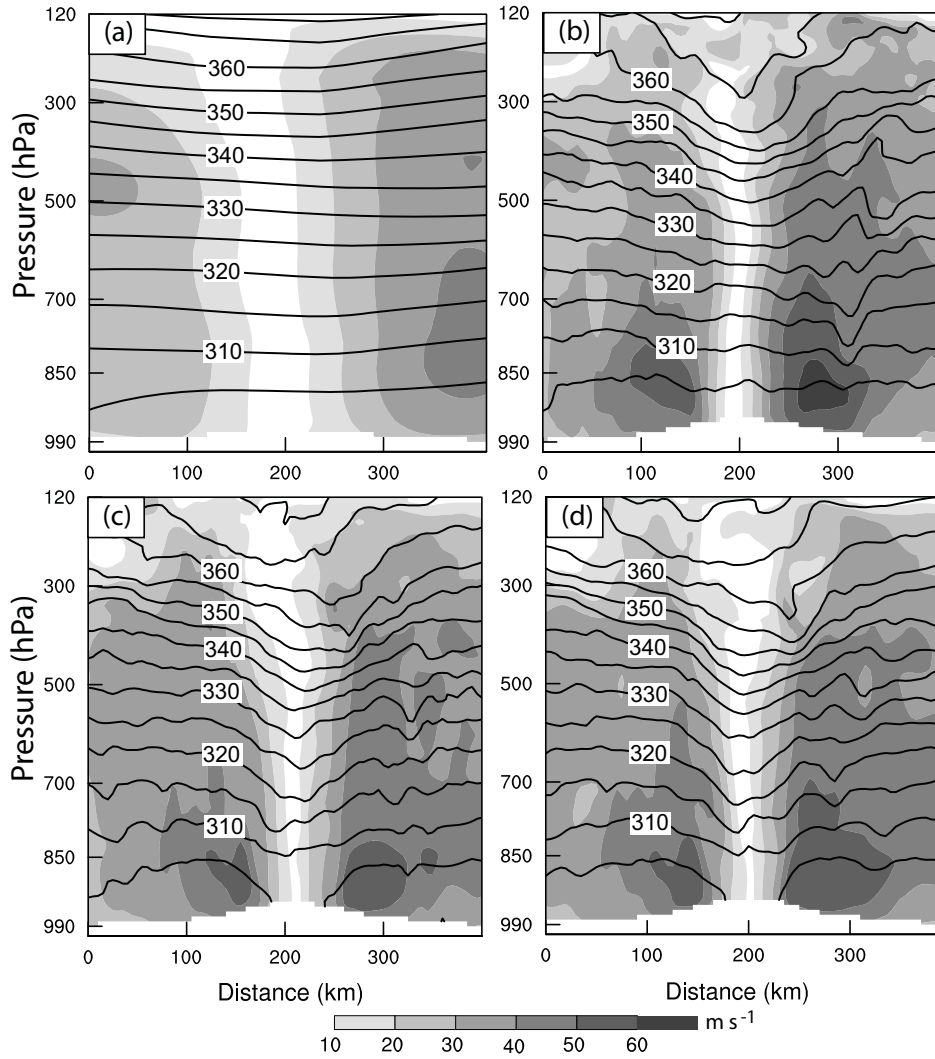


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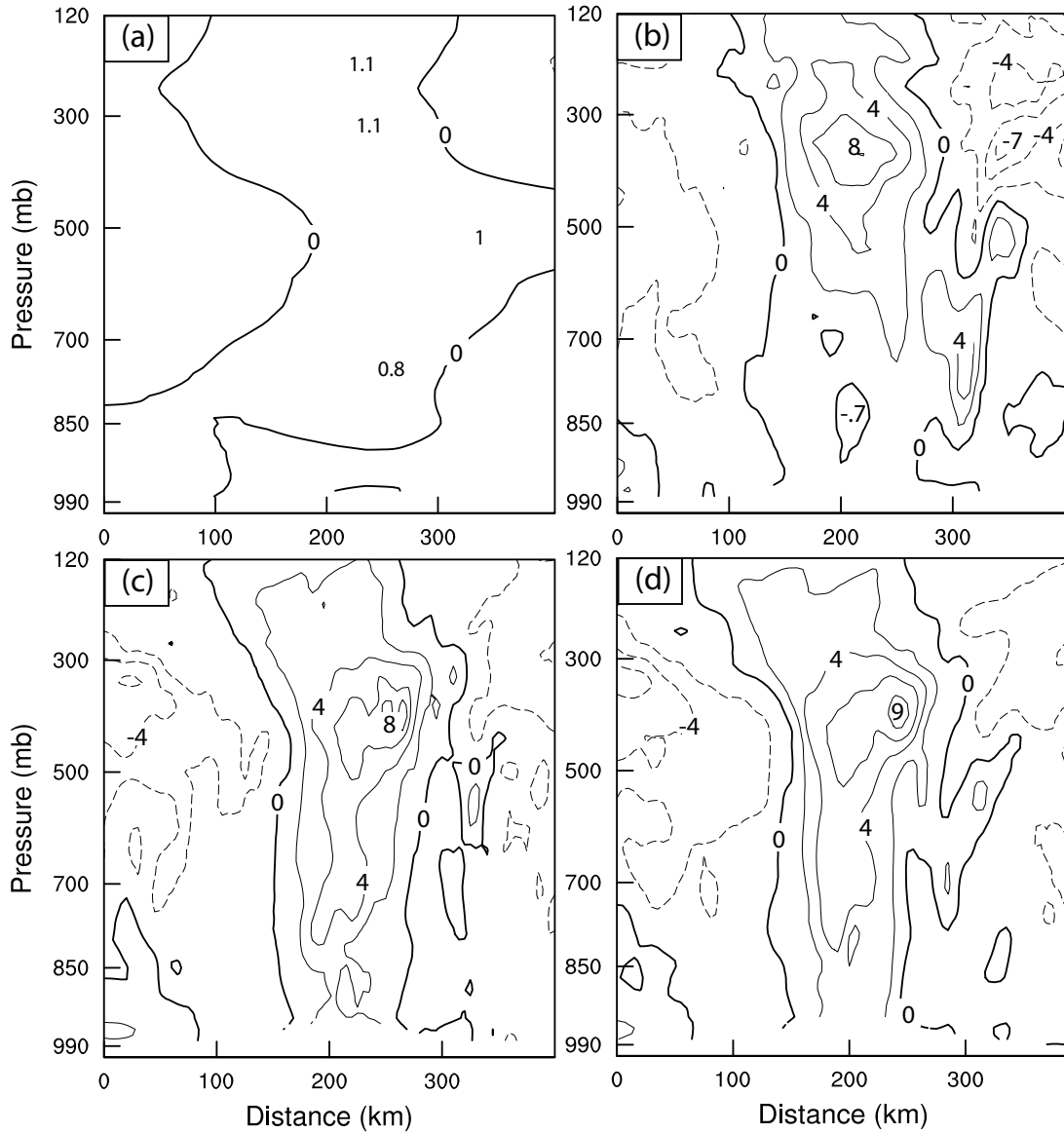
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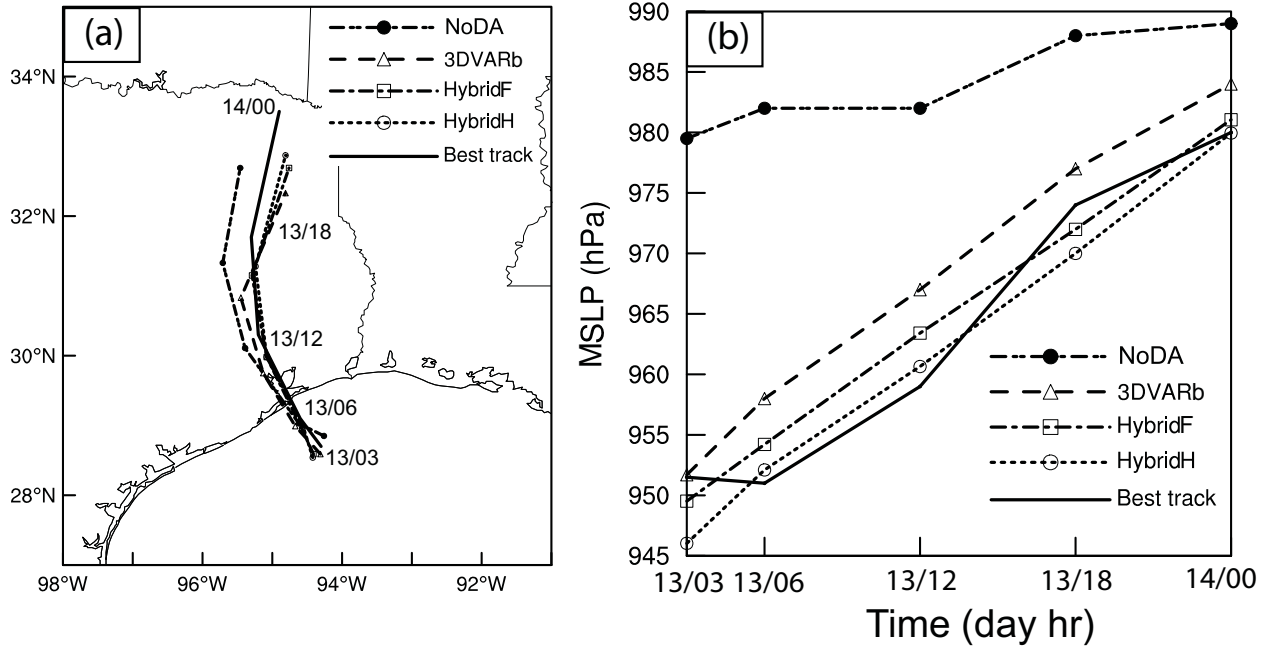
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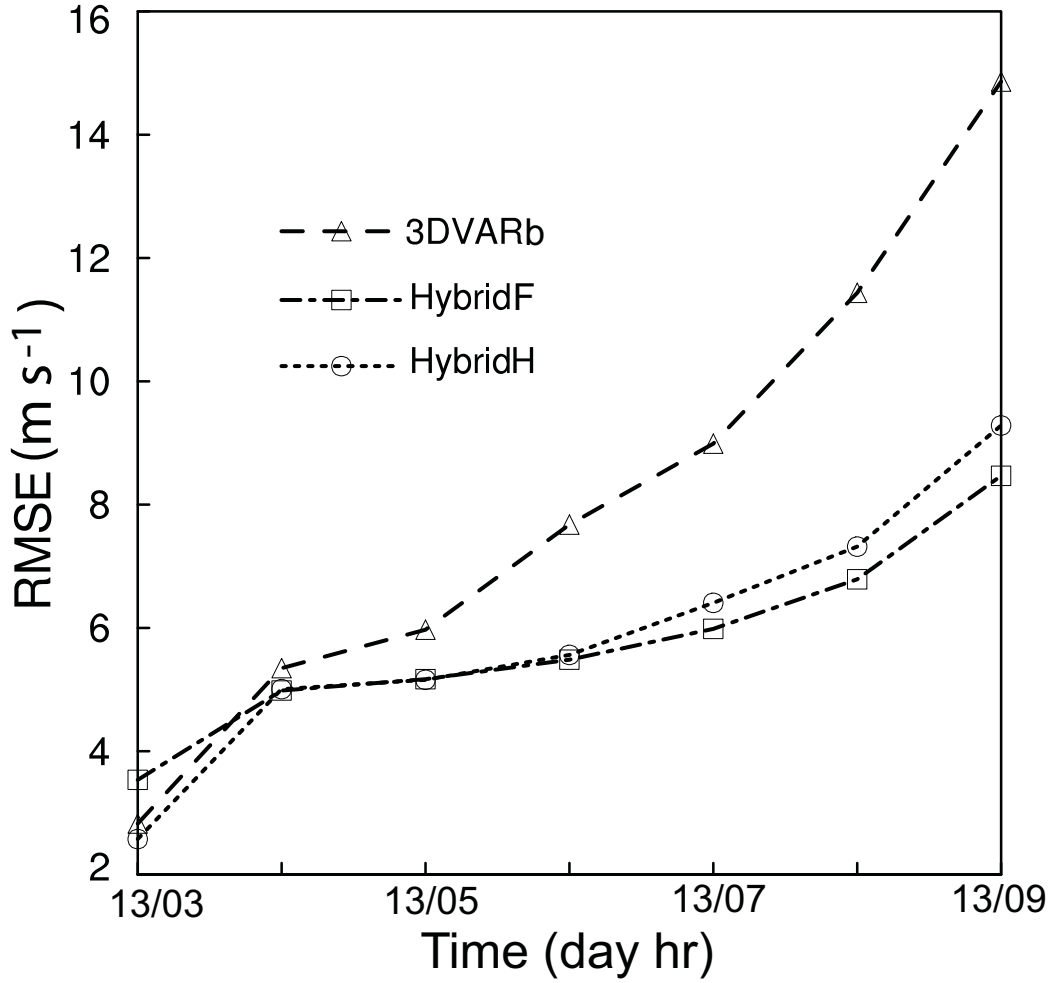
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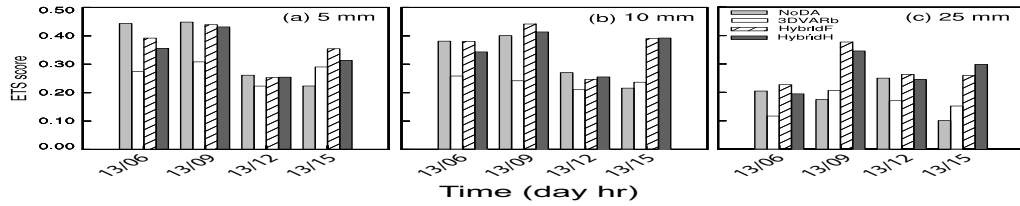


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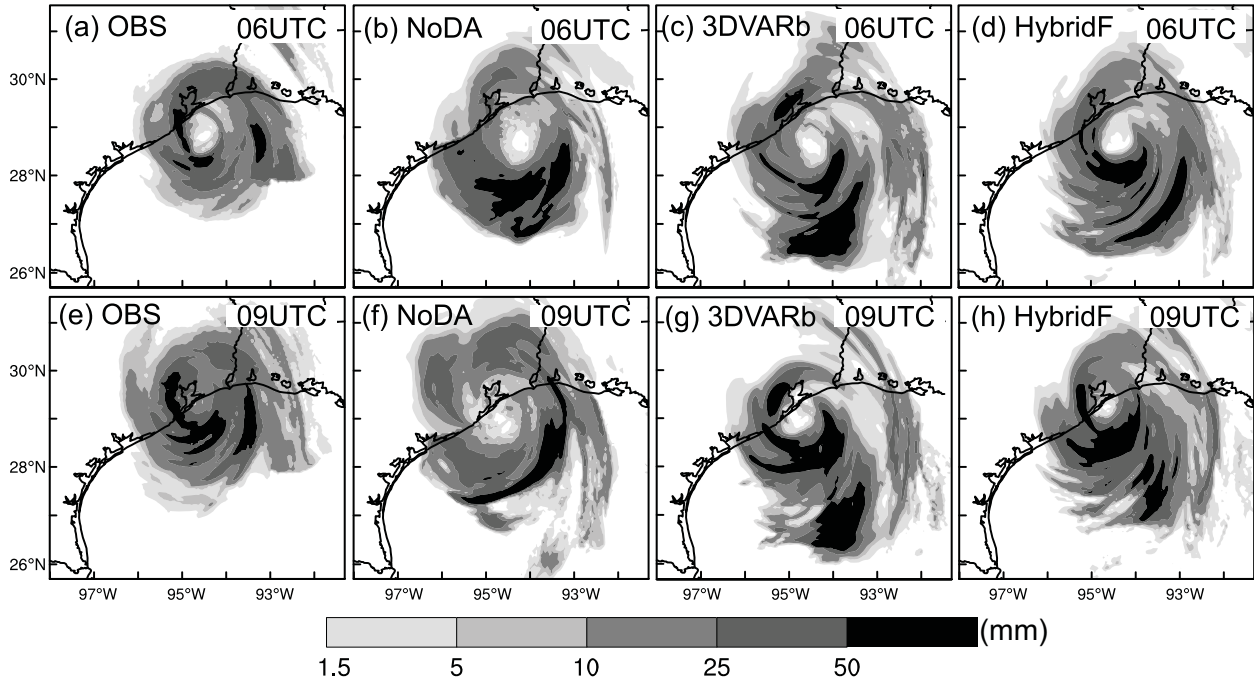


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Fig. 15 Three-hour accumulated precipitation (mm) by (1<sup>st</sup> column) NCEP Stage-IV precipitation analyses, (2<sup>nd</sup> column) NoDA, (3<sup>rd</sup> column) 3DVARb, and (4<sup>th</sup> column) HybridF valid at (top) 0600 and (bottom) 0900 UTC 13 September 2008.